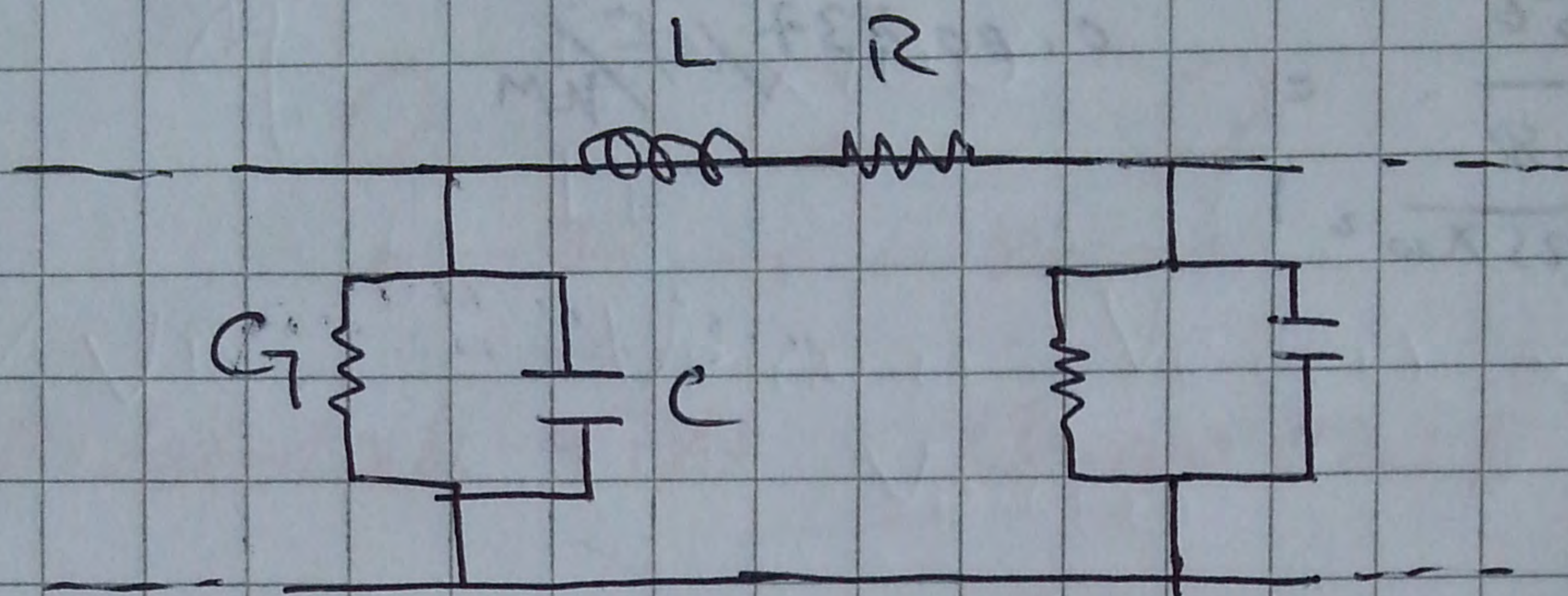


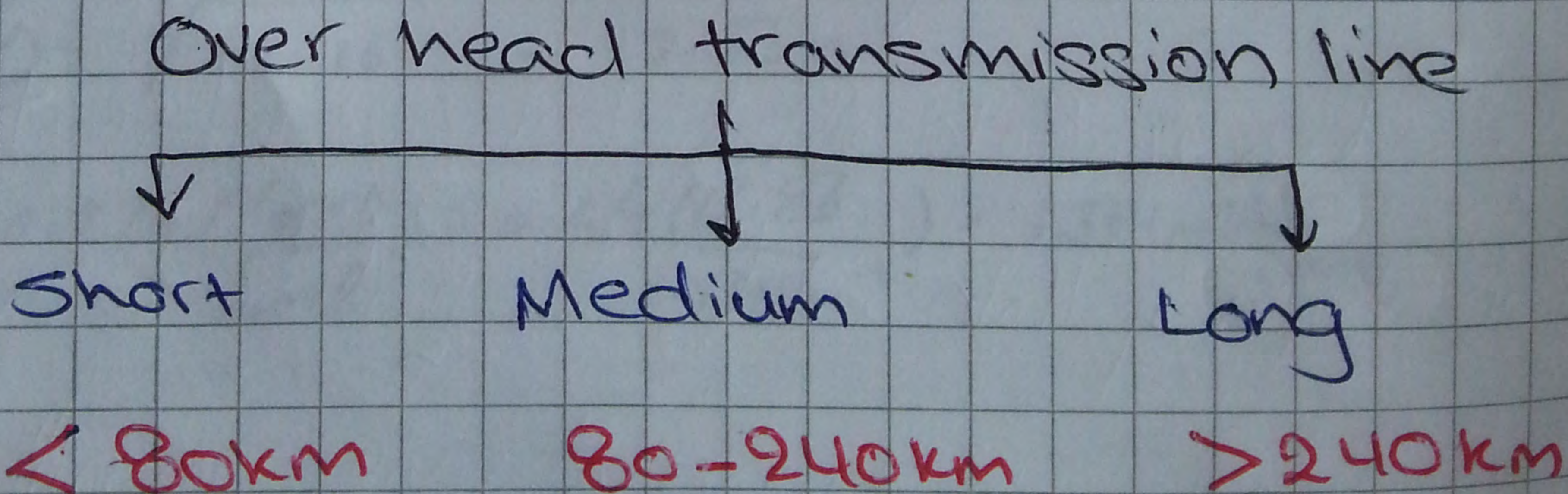
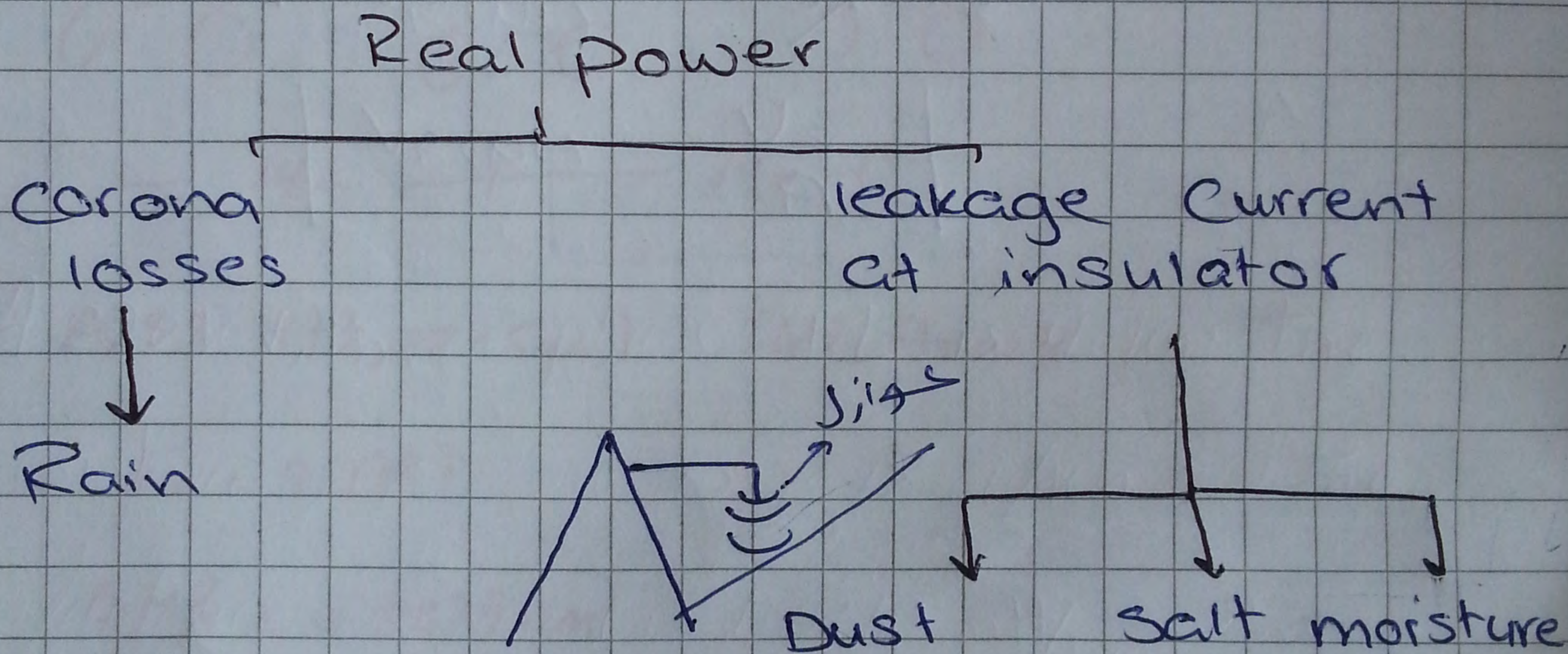
A.G

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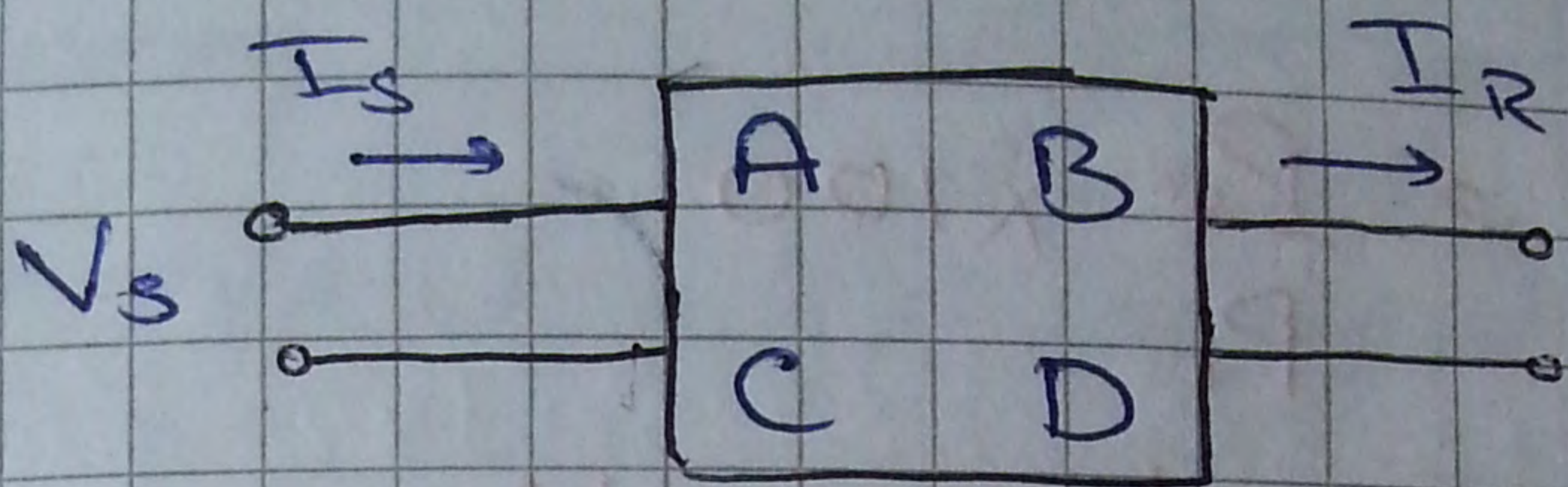
lecture 9



### [Conductance]







Line Parameters

$$V_s = A \cdot V_R + B \cdot I_R$$

$$I_s = C \cdot V_R + D \cdot I_R$$

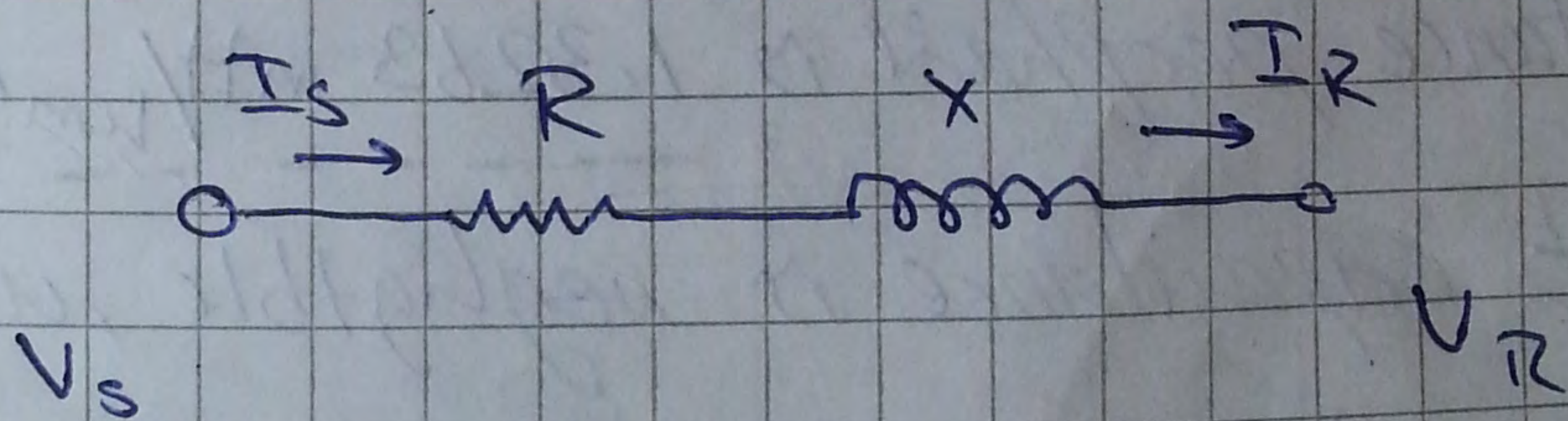
$V_s \triangleq$  sending voltage

$I_s \triangleq$  sending current

$V_R \triangleq$  receiving voltage

$I_R \triangleq$  receiving current

Short line model



phase to neutral

$$Z = R + jX$$

$$V_s = A_s V_R + B_s I_R$$

$$V_s = I_s V_R + Z I_R$$

$$I_s = [0] V_R + [1] I_R$$

$$A = 1 \quad B = Z$$

$$C = 0 \quad D = 1$$



$$\eta = \frac{P_o}{P_i} \times 100$$

$$\%VR = \frac{V_{R(NL)} - V_{R(FL)}}{V_{R(FL)}} \times 100$$

At No load  $I_R = 0$

$$V_s = A V_{R(NL)} + B \times I_R$$

$$\left[ V_{R(NL)} = \frac{V_s}{A} \right]$$

nominal  
voltage

$\frac{1}{\sqrt{3}}$

phase to  
phase

we use phase to neutral

is

is

is

is

is

Ex: A 220 kV, three phase T.L is 40 km the

resistance per phase is 0.15  $\Omega$ /km and the

inductance per phase is 1.3263 mH/km the

shunt capacitance is negligible, use the

short model line to find the voltage and

power at sending end and the voltage regulation

and efficiency when the line is supplying a three



phase load of

power  
Factor

تأخران ولاد

a) 381 MVA at 0.8 pf lagging at 220kV

$V_R$

b) 381 MVA at 0.8 pf leading at 220kV

رأنا لومقلنا  
العكس

$$R = 0.15 \times 40 = 6 \Omega$$

$$X = \omega L = 2\pi(60) \times 1.3263 \times 10^{-3} \times 40 = 20 \Omega$$

$$Z = 6 + j20 = 20.881 \angle 73.3^\circ$$

$$V_R = \frac{220}{\sqrt{3}} = 127 \text{ kV} \angle 0^\circ$$

$$S_{1-\phi} = V_{ph-N} \times I^*$$

$$S_{3\phi} = \sqrt{3} V_{LL} \times I^*$$

$$S_{1-\phi} = \frac{381}{3} = 127 \text{ MVA}$$

$$|I_R| = \frac{127 \times 10^6}{127 \times 10^3} = 1 \text{ kA}$$

$$F_p = \cos \theta \Rightarrow \theta = \cos^{-1}(0.8) = 36.87^\circ$$

$$I_R = 1 \text{ kA} \angle -36.87^\circ$$



$$V_s = A V_R + B I_R$$

$$= 1 \angle 127.2^\circ + 20.88 \angle 73.3^\circ \cdot 1 \angle -36.87^\circ$$

$$= 144.33 \text{ kV} \angle 4.93^\circ$$

$$|V_s| = \sqrt{3} (144.33) = 250 \text{ kV}$$

$$I_s = I_R = 1 \text{ kA} \angle -36.87^\circ$$

$$S_{SC1\phi} = V_{s1} \cdot I_s^*$$

$$= 144.33 \angle 4.93^\circ \cdot 1 \angle -36.87^\circ$$

$$= 144.33 \angle 41.9^\circ$$

$$S_{3\phi} = 3 S_{1\phi} = 432.99 \text{ MVA} \angle 41.9^\circ$$

$$= \underbrace{322.8}_{P_s} + j \underbrace{288.6}_{Q_s}$$

$$P_R = S_R + P$$



$$= 381 \times 0.8 = 304.8 = 304.8 \text{ MW}$$

$$\eta = \frac{304.8}{322.8} \times 100 = 94.4\%$$

$$\%VR = \frac{V_R(NL) - V_R(FL)}{V_R(FL)}$$

$$V_R(NL) = \frac{V_s}{A} - \frac{250}{I} = 250 \text{ kv}$$

$$\%VR = \frac{250 - 220}{220} \times 100 = 13.6\%$$



lecture  
10

at the last example

b) 381 MVA at 0.8 power factor leading at 220 kV

$$Z = 6 + j20 \, \Omega = 20.88 \angle 73.3^\circ$$

$$V_R = \frac{220}{\sqrt{3}} = 127 \text{ kV} \angle 0$$

$$|I_R| = 1 \text{ kA}$$

$$\theta = \cos^{-1}(0.8) = 36.87^\circ$$

$$I_R = 1 \text{ kA} \angle 36.87^\circ$$

$$V_S = 1 \angle 0 + \frac{127}{\text{kV}} \angle 0 + \frac{20.88}{\Omega} \angle 73.3^\circ \times \frac{1}{\text{kA}} \angle 36.87^\circ$$

$$V_S = 121.39 \text{ kV} \angle 9.29^\circ$$

$$\rightarrow |V_{S_{LL}}| = \sqrt{3} (121.39) = 210.26 \text{ kV}$$

$$I_S = I_R = 1 \text{ kA} \angle 36.87^\circ$$

$$S = V_S I_S^*$$

$$= 121.39 \angle 9.29^\circ \times 1 \angle -36.87^\circ$$



$$S = P + jQ$$

$$\begin{aligned} S_{3\phi} &= 3 S_{1\phi} = 364.18 \text{ MVA} \angle -27.58^\circ \\ &= \underbrace{322.8 \text{ MW}}_P - j \underbrace{168.0 \text{ MVAR}}_Q \end{aligned}$$

$$\gamma = \frac{P_o}{P_i} = \frac{P_R}{P_S} \times 100$$

$$\begin{aligned} P_S &= S \cos \phi \\ &= 381 \times 0.8 = 304.8 \text{ MW} \end{aligned}$$

$$= \frac{304.8}{322.8} \times 100 = 94.4\%$$

$$V_R(\text{V}) = 210.26$$

$$VR\% = \frac{210.26 - 220}{220} \times 100 = -4.43\%$$

→ inductive load  $F_p$  lagging

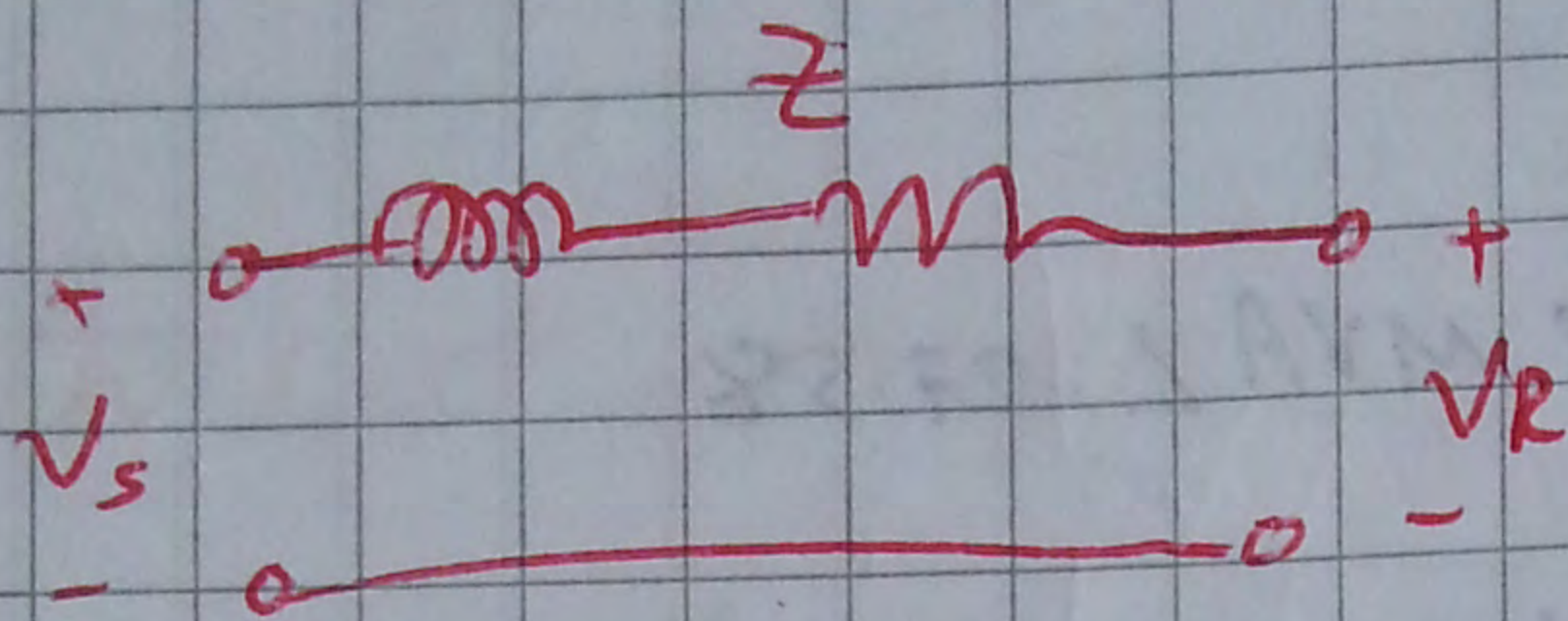
$$V_S > V_R$$

→ Capacitive load  $F_p$  leading

$$V_S < V_R$$



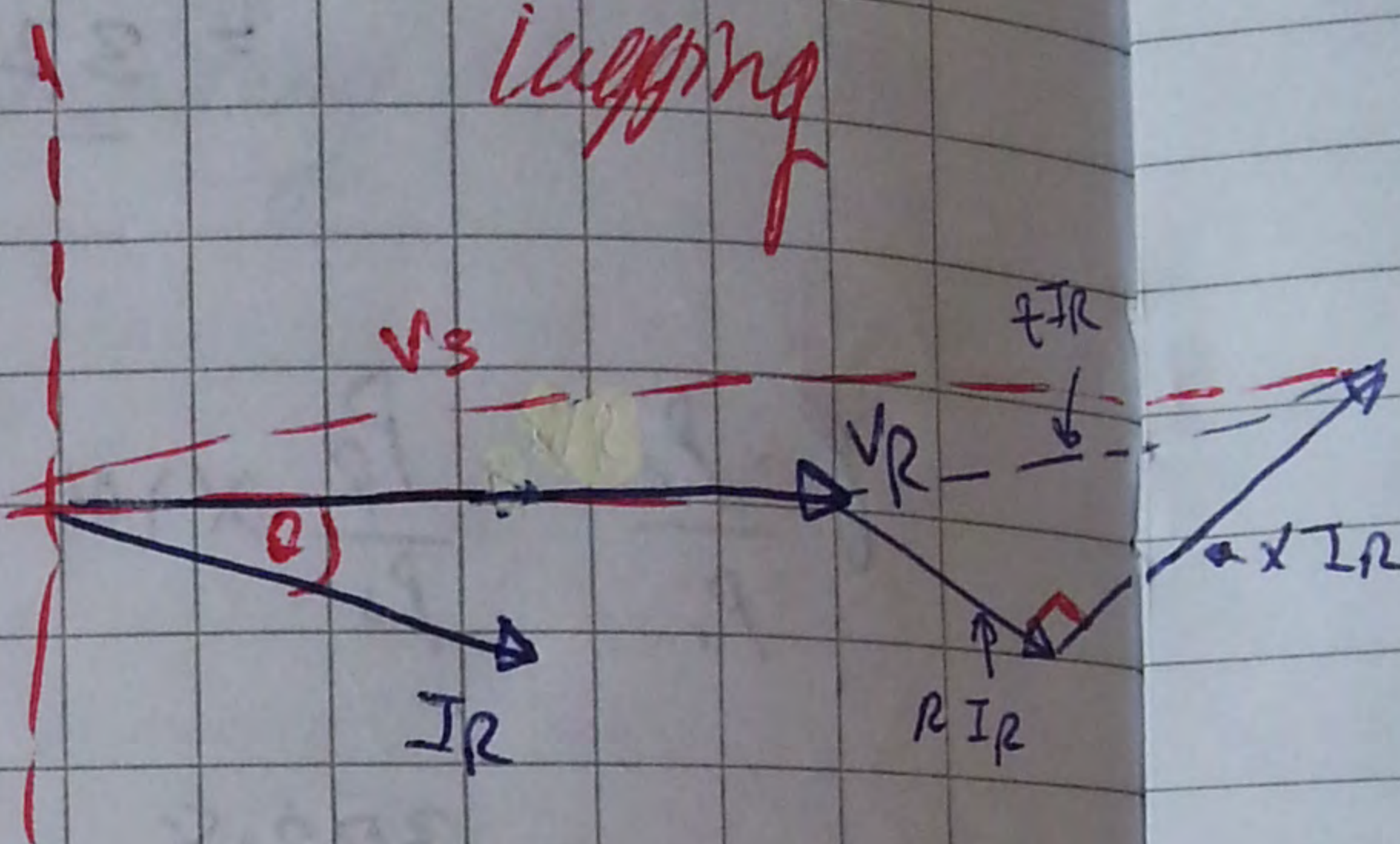
X



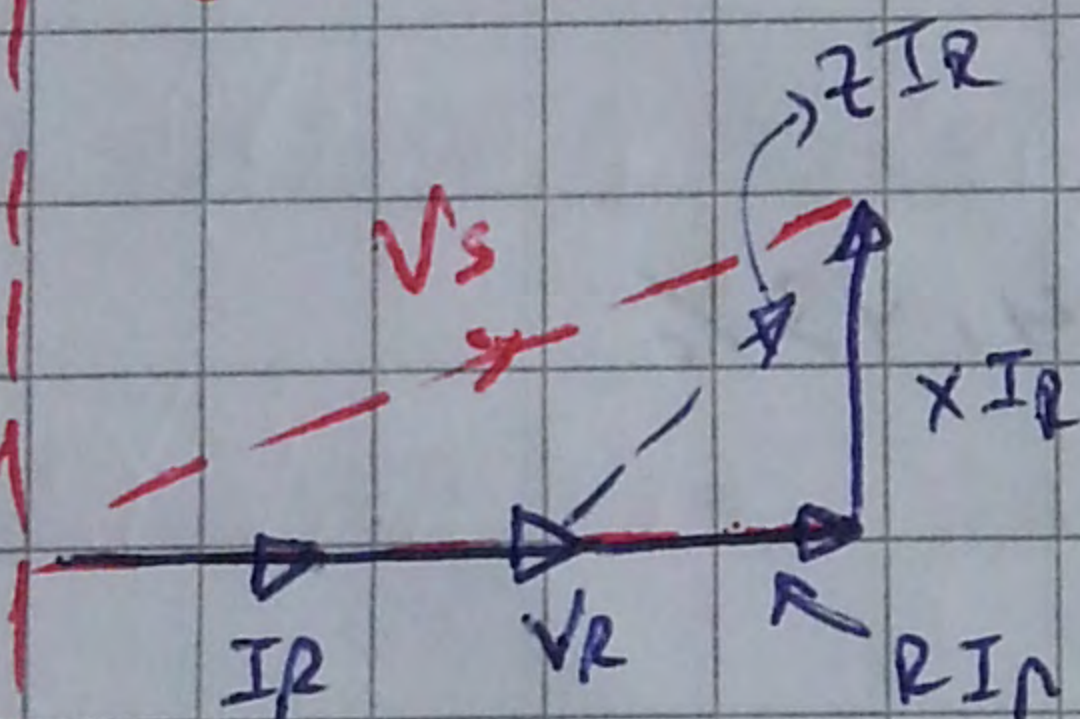
$$V_s = V_R + Z I_R$$

$$= V_R + R I_R + j X I_R$$

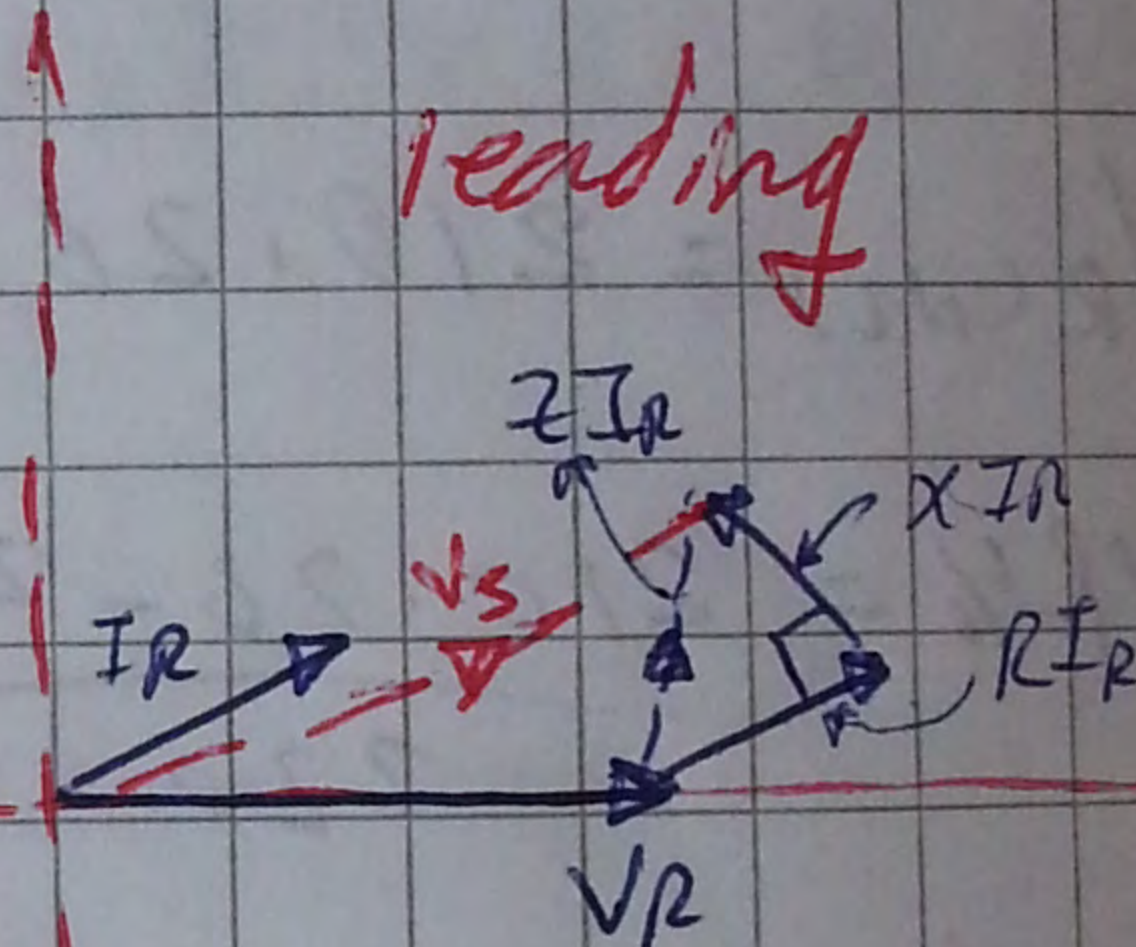
lagging



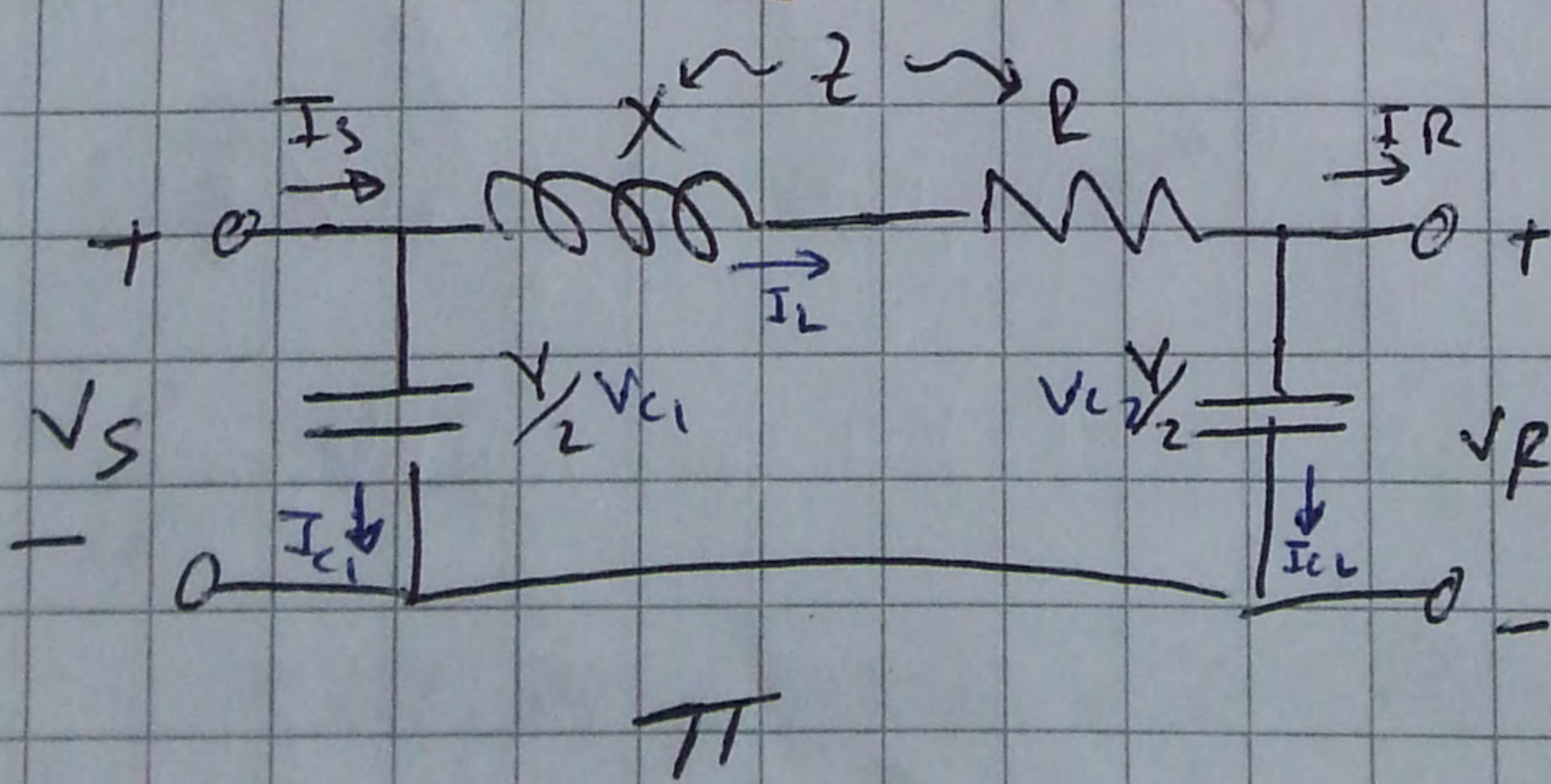
(unity) "in phase"  
FP 0



leading



## Medium Line Model





$$\begin{aligned}
 V_s &= V_R + Z I_L \\
 &= V_R + Z (I_{C_2} + I_R) \\
 &= V_R + Z \left( \frac{Y}{2} V_R + I_R \right)
 \end{aligned}$$

$$= V_R + \frac{Z Y}{2} V_R + Z I_R$$

$$= \underbrace{\left( 1 + \frac{Z Y}{2} \right)}_A V_R + \underbrace{Z I_R}_B$$

$$I_s = I_{C_1} + I_L$$

$$= \frac{Y}{2} V_s + (I_{C_2} + I_R)$$

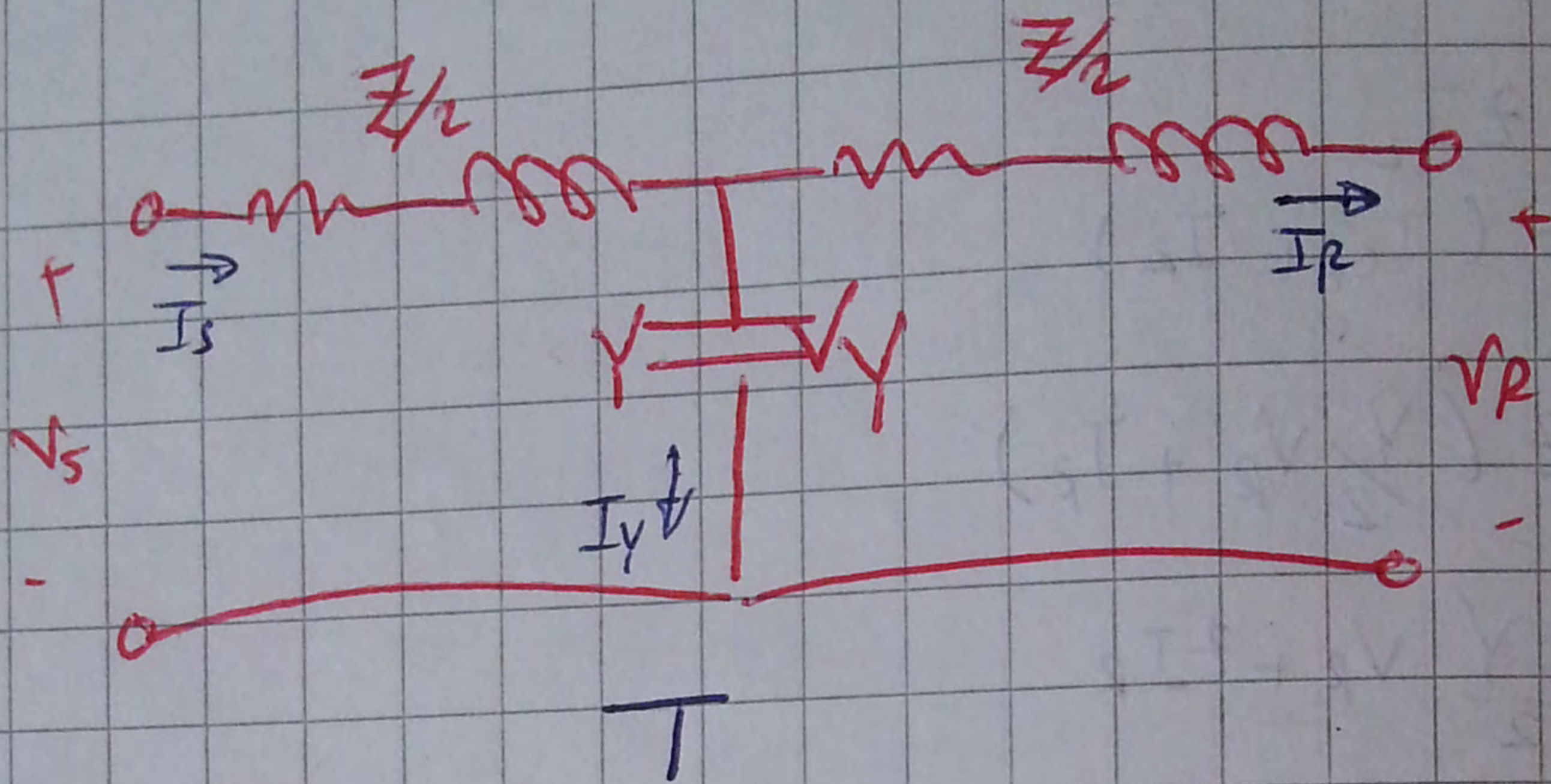
$$= \frac{Y}{2} V_s + \frac{Y}{2} V_R + I_R$$

$$= \frac{Y}{2} \left[ V_R + \frac{Z Y}{2} V_R + Z I_R \right] + \frac{Y}{2} V_R + I_R$$

$$= Y V_R + \frac{Z Y^2 V_R}{4} + \frac{Z Y I_R}{2} + I_R$$

$$I_s = \underbrace{Y \left( 1 + \frac{Z Y}{4} \right)}_C V_R + \underbrace{\left( 1 + \frac{Z Y}{2} \right)}_D I_R$$





$$I_s = I_R + I_Y$$

$$= I_R + Y V_Y$$

$$= I_R + Y \left[ V_R + \frac{Z}{2} I_R \right]$$

$$= Y V_R + I_R + \frac{Z Y}{2} I_R$$

$$I_s = Y V_R + \underbrace{\left( 1 + \frac{Z Y}{2} \right)}_D I_R$$

$$V_s = V_Y = \frac{Z}{2} I_s$$

$$= V_R + \frac{Z}{2} I_R + \frac{Z}{2} \left[ Y V_R + I_R + \frac{Z Y}{2} I_R \right]$$

$$= V_R + \frac{Z}{2} V_R + \frac{Z}{2} I_R + \frac{Z^2 Y}{4} I_R$$

$$= \underbrace{\left( 1 + \frac{Z Y}{2} \right)}_A V_R + \underbrace{\frac{Z}{2} \left( 1 + \frac{Z Y}{2} \right)}_B I_R$$



✓ Ex 8-

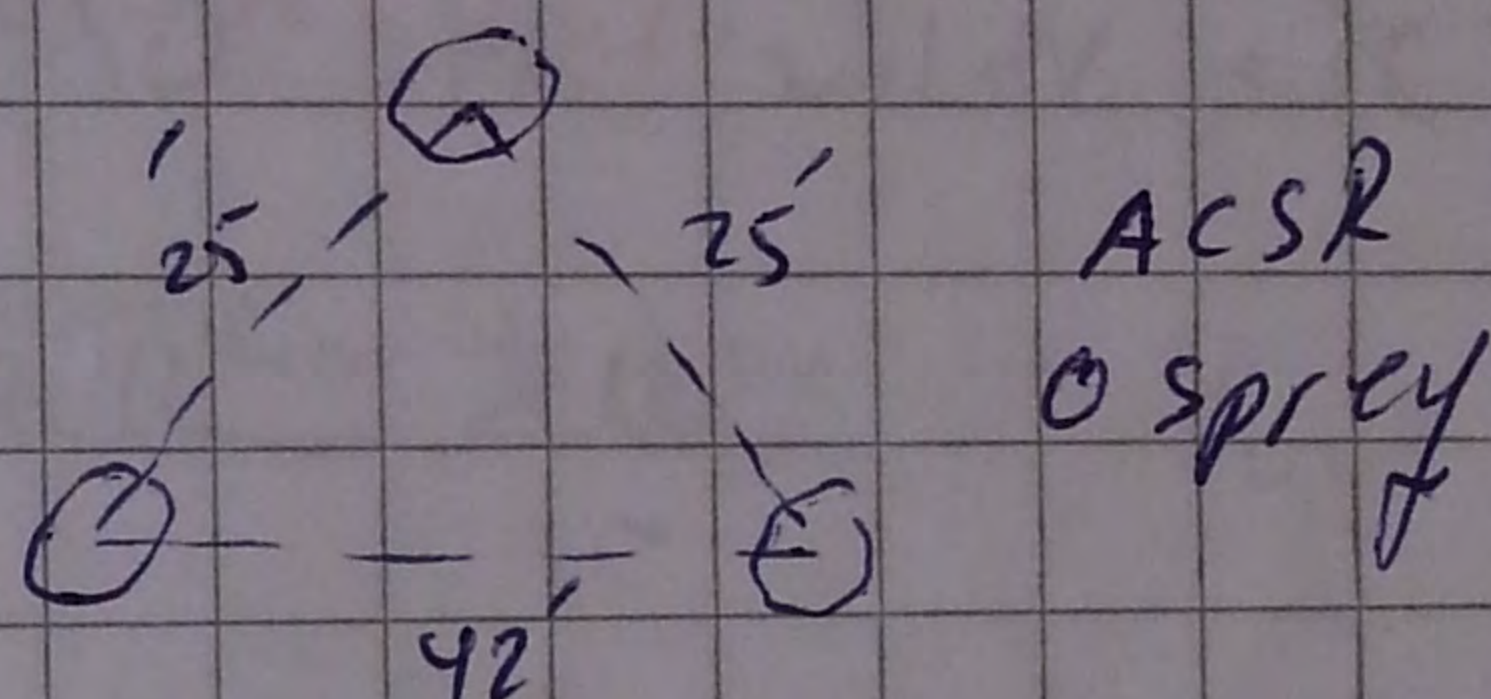
a) Determine the capacitance to neutral in  $\mu\text{F}/\text{mi}$   
 and the capacitive reactance in  $\Omega \cdot \text{mi}$  <sup>to neutral</sup>

b) If the line is 150 mile long, find the capacitance  
 to neutral and the capacitive reactance of the line

From the table  $r = \frac{D}{2} = \frac{0.879}{2} =$

$r = 0.4395 \text{ m}$

$r = \frac{0.4395}{12} = 0.036625 \text{ ft}$



a)  $C = \frac{2\pi\epsilon_0}{\ln\left(\frac{GMD}{r}\right)} = \frac{2\pi\epsilon_0}{\ln\left(\frac{\sqrt[3]{25+25+42}}{0.036625}\right)} = 8.3 \text{ pF/m}$

$C = 1609 \times 8.3 \text{ p} = 0.0134 \mu\text{F}/\text{mile}$

$X_c = \frac{1}{\omega C} = \frac{1}{2\pi f C} = 198.5 \text{ k}\Omega \cdot \text{mile}$

b)  $C = 2.01 \mu\text{F}$

$X_c = 1.319 \text{ k}\Omega$



lecture  
①

تابع العال السابق

البيانات في  $X_c$  هي

$$X_c = X_a + X_b$$

$$X_a = 0.0981 \text{ Mod. mile} \quad \leftarrow \text{من الجدول}$$

$$X_b = \text{value at GMD} = 29.72$$

وبما أن هذه القيمة لا توجد في الجدول

① Interpolation

② تطبيق الصيغة

$$X_b = 0.06831 \log(d)$$

$$= 0.06831 \log(29.72)$$

$$= 0.1006 \text{ Mod. mile}$$

$$\frac{30 - 29}{0.1009 - 0.0999} = \frac{29.72 - 29}{X - 0.0999} \Rightarrow X = 0.101 \pm 0.01006$$



$$X_c = 0.981 + 0.1006 = 198.7 \text{ k}\Omega \cdot \text{mile}$$

Find the total charge current and the total charge in mega volt amperes

$$I_{ch} = j\omega C V_{\text{phase to neutral}}$$

Capacitance to neutral

assume 3  $\phi$  at 220kV Line to line

$$V_{LL} = \sqrt{3} V_{ph-n}$$

$$|I_{ch}| = \frac{2\pi(60)(2.01\mu) \times 220\text{k}}{\sqrt{3}}$$

$$|I_{ch}| = 96.185 \text{ A}$$

$$S = P + jQ$$

$$Q_{3\phi} = \sqrt{3} V_{LL} I_{ch} \sin \theta$$

$\rightarrow I_{ch}$

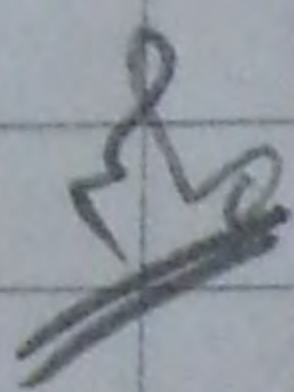
$$= \sqrt{3} (220\text{k}) (96.185) = 36.03 \text{ MVAR}$$

$$Q_{1\phi} = \frac{V_{ph-n}}{\sqrt{3}} I_{ch} \sin \theta$$

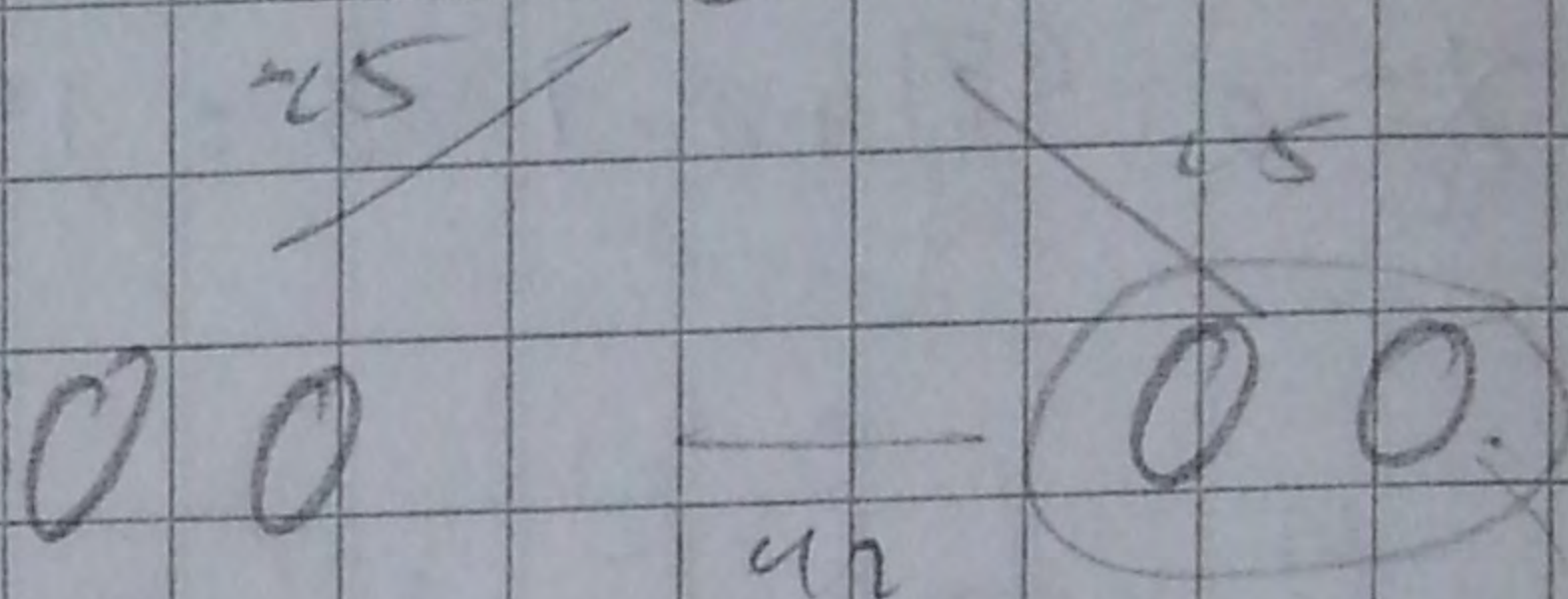
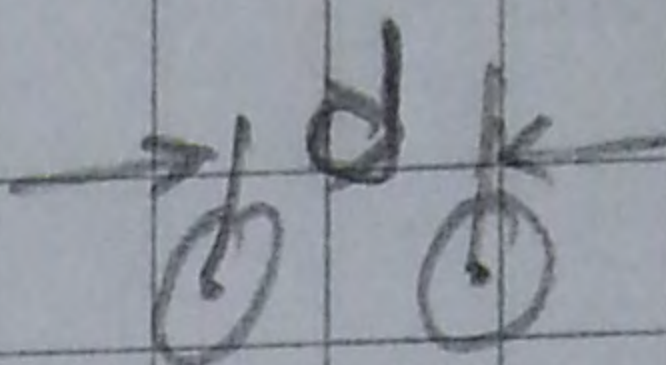
$$= \frac{220}{\sqrt{3}} (96.185)$$

$$\Rightarrow Q_{3\phi} = 3 Q_{1\phi}$$





For



From table

$$R_{ac} \text{ at } 50^\circ\text{C} = 0.1843 \Omega / \text{mile}$$

60Hz

$$C = \frac{2\pi\epsilon_0}{\ln\left(\frac{GMD}{GMR_c}\right)}$$

$$GMR_c = r$$

$$\sqrt{rxd}$$

$$\sqrt[2]{rd^2}$$

1 ✓ and  
2 ✓  
3 ✓

GM

capacitance double

c'

a

(a x a) / 2

a'

b'

c

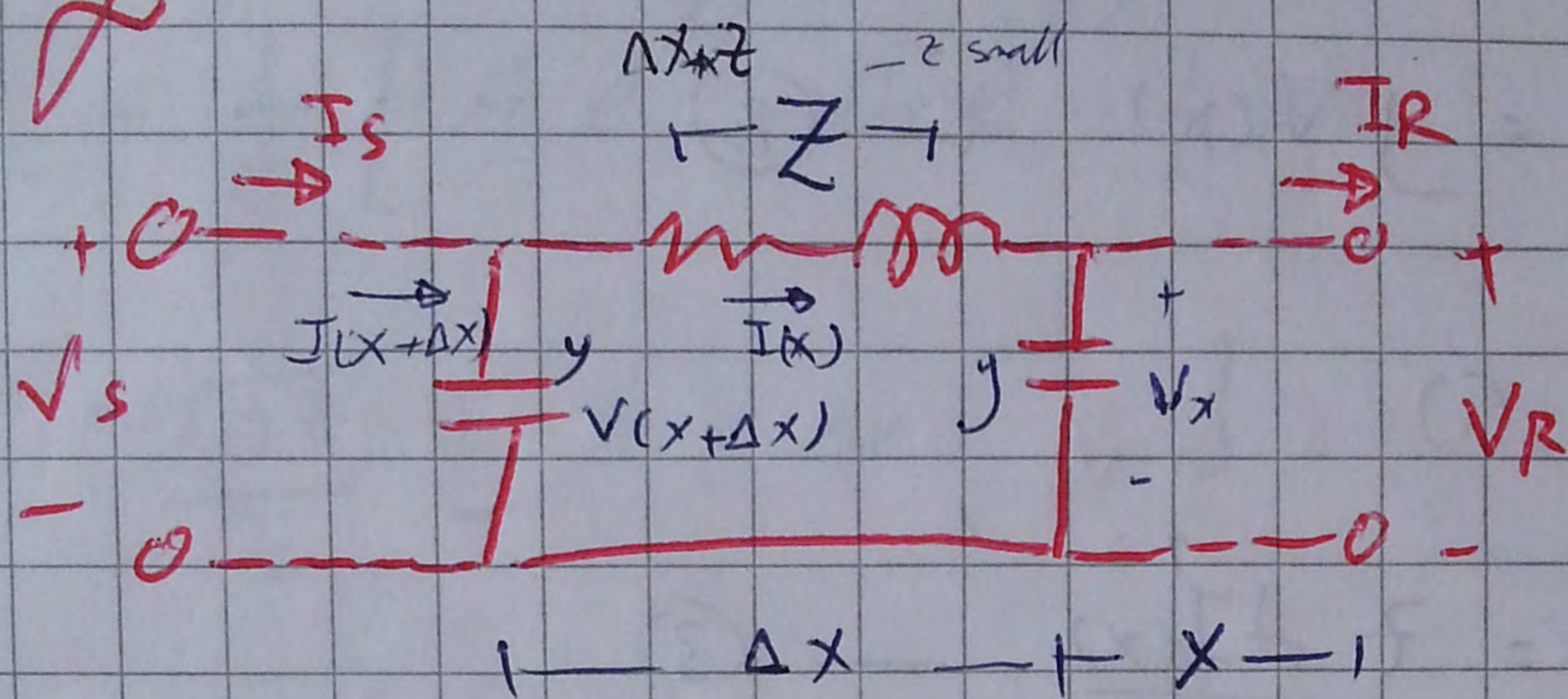
b

inductance  
a' b' c b'



lecture  
(12)

# Long Line Model :-



$Z =$  series impedance / unit length

$y =$  shunt admittance

$$V(x+\Delta x) = V(x) + \Delta x Z I(x)$$

$$Z I(x) = \frac{V(x+\Delta x) - V(x)}{\Delta x}$$

$$\Delta x \rightarrow 0$$

$$\frac{dV(x)}{dx} = -Z I(x) \quad \text{--- (1)}$$

$$I(x+\Delta x) = I(x) + \Delta x y V(x+\Delta x)$$

$$\frac{I(x+\Delta x) - I(x)}{\Delta x} = y V(x+\Delta x)$$



$$\Delta x \rightarrow 0$$

$$\frac{dI(x)}{dx} = -\gamma V(x) \quad \text{--- (2)}$$

diff eq (1)

$$\frac{d^2 V(x)}{dx^2} = \gamma \frac{dI(x)}{dx} \quad \text{--- (3)}$$

Sub (3) in (2)

$$\frac{d^2 V(x)}{dx^2} = -\gamma^2 V(x)$$

$$\textcircled{1} \quad \frac{d^2 V(x)}{dx^2} + \gamma^2 V(x) = 0 \quad \text{diff equation in order 2}$$

$$V(x) = A_1 e^{\gamma x} + A_2 e^{-\gamma x}$$

$\gamma = \sqrt{ZY} \equiv \text{propagation constant}$

$$\gamma = \alpha + j\beta$$

$\alpha$  attenuation constant

$\beta$  phase constant



$$I(x) = \frac{1}{Z} \frac{dV(x)}{dx}$$

$$= \frac{1}{Z} [A_1 e^{\gamma x} - A_2 e^{-\gamma x}] \gamma$$

$$= \frac{\sqrt{Y Z}}{Z} [ \quad \quad ]$$

$$= \sqrt{\frac{Y}{Z}} [ \quad \quad ]$$

$$Z_c = \sqrt{\frac{Z}{Y}}$$

characteristic impedance

$$I(x) = \frac{1}{Z_c} [A_1 e^{\gamma x} - A_2 e^{-\gamma x}] \quad - (2)$$

To find  $A_1$  and  $A_2$

$$\text{at } x=0 \Rightarrow V(x) = V_R, \quad I(x) = I_R$$

$$V_R = A_1 + A_2$$

$$I_R = \frac{1}{Z_c} (A_1 - A_2)$$

$$\Rightarrow A_1 = \frac{V_R + Z_c I_R}{2}$$

$$, A_2 = \frac{V_R - Z_c I_R}{2}$$



Long model more accurate than midium model  
 midium = direct list      Long = all the data

$$V(x) = \left( \frac{V_R + Z_C I_R}{2} \right) e^{\gamma x} + \left( \frac{V_R - Z_C I_R}{2} \right) e^{-\gamma x}$$

$$I(x) = \frac{1}{Z_c} \left[ \left( \frac{V_R + Z_c I_R}{2} \right) e^{\gamma x} - \left( \frac{V_R - Z_c I_R}{2} \right) e^{-\gamma x} \right]$$

$$V(x) = \overset{\text{Cosh}}{\left( \frac{e^{\gamma x} + e^{-\gamma x}}{2} \right)} V_R + Z_c \left( \frac{e^{\gamma x} - e^{-\gamma x}}{2} \right) I_R \overset{\text{sinh}}$$

$$I(x) = \frac{1}{Z_0} \left( \frac{e^{\gamma x} - e^{-\gamma x}}{2} \right) \sqrt{R} + \left( \frac{e^{\gamma x} + e^{-\gamma x}}{2} \right) I_R$$

Line length =  $L = x$

$$V(\ell) = V_s, \quad I(\ell) = I_s$$

$$V_s = \cosh(\gamma l) V_R + Z_0 \sinh(\gamma l) I_R$$

$$I_s = \frac{1}{Z_c} \sinh(\gamma l) V_R + \cosh(\gamma l) I_R$$

$$(AD \cdot BC = 1)$$



$$\bar{Z} = Z_c \sinh(\gamma l)$$

$$= \frac{\sqrt{Z}}{\sqrt{Y}} \times \frac{\sqrt{Z}}{\sqrt{Y}} \times \frac{1}{l} \sinh(\gamma l)$$

$$= \frac{Z l}{\gamma l} \sinh(\gamma l)$$

$$\bar{Z} = \frac{Z}{\gamma l} \sinh(\gamma l)$$

$$1 + \frac{Z \bar{Y}}{2} = \cosh(\gamma l)$$

$$1 + \frac{\bar{Y} Z_c \sinh(\gamma l)}{2} = \cosh(\gamma l)$$

$$\frac{\bar{Y}}{2} = \frac{\cosh(\gamma l) - 1}{Z_c \sinh(\gamma l)}$$

$$= \frac{1}{Z_c} \tanh\left(\frac{\gamma l}{2}\right)$$

$$\boxed{\frac{\bar{Y}}{2} = \frac{Y}{2} \frac{\tanh(\gamma l/2)}{(\gamma l/2)}}$$



$$\frac{2\pi}{\omega} = \frac{2\pi}{2\pi f} =$$

Voltage and current waves :-

lecture  
(13)

velocity of propagation  $v = \frac{\omega}{\beta}$

wave length  $\lambda = \frac{2\pi}{\beta} = v/f$

Ex 8 - A single cat 60 Hz T.L, is 370 km

(230 mile) long. The conductors are Rook

with flat horizontal, spacing 7.25 m (23.8 ft)

between conductors, the load on the line is

125 MW at 215 kV with 100% PF

Find the voltage, current and power at

sending end and % V.R of the line, Also

determine the wave length and velocity of

propagation of the line



$$z = \frac{\Omega}{\text{unit length}}$$

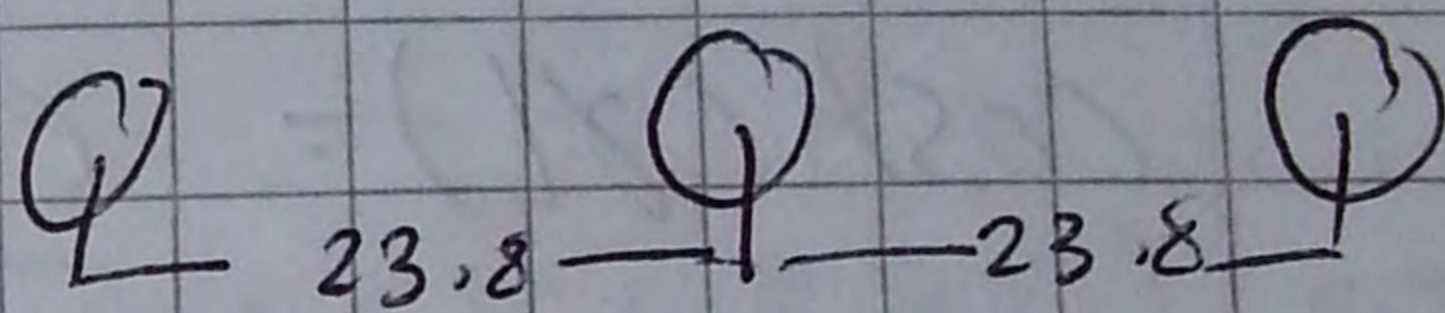
$$Z = \Omega$$

$$\gamma = \alpha + j\beta = \sqrt{zy} \Rightarrow \gamma l = \sqrt{zy}$$

$$z = r + jX_L$$

From table  $r$  (AC at  $50^\circ\text{C}$ )

$$r = 0.1603 \text{ } \Omega/\text{mile}$$



$$X_L = X_a + X_d \xrightarrow{\text{For GMD}} = 0.415 + 0.4127 = 0.8277 \text{ } \Omega/\text{mile}$$

$$\text{GMD} = \sqrt{23.8 \times 23.8 \times (23.8 \times 2)} = 30 \text{ ft}$$

$$Z = 0.1603 + j0.8277 = 0.8431 \angle 79.04^\circ \text{ } \Omega/\text{mile}$$

Zero S,  $\omega = 1$

$$y = g + jb \Rightarrow y = jb = j \frac{1}{X_c} = j \frac{1}{X_a + X_d}$$

$$y = j \frac{1}{0.0950 + 0.1009}$$

$$X_a \text{ From table} = 0.0950 \text{ M}\Omega/\text{mi}$$

$$X_d = 0.1009 \text{ M}\Omega/\text{mile}$$

$$y = 5.105 \times 10^{-6} \angle 90^\circ \text{ S/mile}$$



تحت الجذر الزوايا تنجمع وتنفك على 2

$$\gamma l = l \sqrt{zy} = 230 \sqrt{0.8431 \times 5.105 \times 10^{-6}} \angle \frac{79.04 + 90}{2}$$

$$= 0.47722 \angle 84.52^\circ = 0.456 + j0.475$$

$$\gamma l = \underbrace{0.456}_{\alpha l} + j \underbrace{0.475}_{\beta l \equiv \text{rad}}$$

rad  $\rightarrow$  degree

$$\frac{0.475 \times 180}{\pi} = 27.22^\circ$$

$$\cosh(\gamma l) = \frac{e^{\gamma l} + e^{-\gamma l}}{2}$$

$$= \frac{1}{2} e^{\alpha l} \angle \beta l + \frac{1}{2} e^{-\alpha l} \angle -\beta l$$

$$= \frac{1}{2} e^{0.456} \angle 27.22^\circ + \frac{1}{2} e^{-0.456} \angle -27.22^\circ$$

$$\sinh(\gamma l) = \frac{e^{\gamma l} - e^{-\gamma l}}{2} = 0.8902 + j0.0209 = 0.8904 \angle 1.34^\circ$$

$$\sinh(\gamma l) = \frac{1}{2} e^{\alpha l} \angle \beta l - \frac{1}{2} e^{-\alpha l} \angle -\beta l$$

$$= 0.0406 + j0.4579 = 0.4597 \angle 84.93^\circ$$

$$V_R = \frac{215}{\sqrt{3}} \angle 0^\circ = 124.13 \angle 0^\circ \text{ kV}$$

$$P_{3\phi} = \sqrt{3} I_L V_L \text{ p.f.}$$



$$I = \frac{125 \times 10^6}{\sqrt{3} \times 215 \times 10^3 \times 1} = 335.7 \text{ A } \angle 0^\circ$$

$$Z_c = \sqrt{\frac{z}{y}} = \sqrt{\frac{0.8431}{5.105 \times 10^{-6}}} \angle \frac{79.04 - 90}{2}$$

$$Z_c = 406.4 \angle -5.46 \Omega$$

$$V_s = (\overset{\text{cosh}(17.1)}{0.8907 \angle 1.34^\circ}) \left[ \overset{VR}{124.13 \angle 0^\circ} \times 10^3 \right] + (\overset{Z_c}{406.4 \angle -5.84^\circ}) \left[ \overset{\text{sinh}(17.1)}{0.4597 \angle 84.93^\circ} \right]$$

$$V_s = 137.86 \angle 27.69 \text{ kV}$$

$$[335.7 \angle 0^\circ] \overset{I_R}{\downarrow}$$

$$|V_s|_{L.L} = 137.86 \sqrt{3} = 238.8 \text{ kV}$$

$$I_s = \frac{1}{406.4 \angle -5.84^\circ} * 0.4597 \angle 84.93^\circ + 124.13 \angle 0^\circ + 0.8907 \angle 1.34^\circ * 0.3357 \angle 0^\circ$$

$$= 332.31 \angle 26.33 \text{ A}$$

$$P_s = \sqrt{3} V_s I_s \text{ Pf}_s$$

$$\text{Pf}_s = \cos(27.77 - 26.33) = 0.9997 \approx 1.0$$

$$P_s = \sqrt{3} \left( \underset{\text{kV}}{238.8} \right) \left( \underset{\text{kA}}{0.3323} \right) (1) = 137.14 \text{ MW}$$



$$\% VR = \frac{V_{R(NL)} - V_{R(FL)}}{V_{R(FL)}} \times 100$$

$$V_{R(NL)} = \frac{V_s}{A} = \frac{137.86}{0.8904} = 154.83 \text{ kV}$$

$$\% VR = \frac{154.83 - 124.13}{124.13} \times 100 = 24.7 \%$$

$$\beta = \frac{0.475}{230} = 0.002065 \text{ rad/mi}$$

$$v = \frac{\omega}{\beta} = \frac{2\pi(60)}{0.002065} = 182580 \text{ mi/sec}$$

$$\lambda = \frac{v}{f} = \frac{182580}{60} = 3043 \text{ mile}$$

Ex 8 Find the equivalent  $\pi$  circuit for the line described in previous example and compare it with the normal  $\pi$  circuit

$$\bar{Z} = Z_L \sinh(\gamma L) = (406.41 \angle -5.48^\circ)(0.4597 \angle 84.93^\circ)$$

$$\bar{Z} = 186.82 \angle 79.45^\circ \Omega$$



$$\bar{Y}_{\frac{1}{2}} = \frac{1}{Z_0} \tanh\left(\frac{\gamma l}{2}\right) = \frac{1}{Z_0} \cdot \frac{\cosh(\gamma l) - 1}{\sinh(\gamma l)} = \bar{Z}$$

$$= \frac{(0.8902 + j0.0209) - 1}{186.82 \angle 79.45^\circ} = 0.000599 \angle 89.82^\circ$$

$$Z = Z_l = 0.8431 \angle 79.04^\circ + 230 = 193.9 \angle 79.04^\circ$$

$$\frac{Y}{2} = \frac{Y_{xl}}{2} = \frac{5.105 \times 10^{-6} \angle 90^\circ \times 230}{2}$$

$$= 0.000587 \angle 90^\circ$$

$$Z > \bar{Z} \quad \text{by } 3.8\%$$

$$\frac{Y}{2} < \bar{Y}_{\frac{1}{2}} \quad \text{by } 2\%$$

the  
are

84.93°



lecture  
(14)

$$V(x) = \cosh(\gamma x) V_R + Z_c \sinh(\gamma x) I_R$$

$$I(x) = \frac{1}{Z_c} \sinh(\gamma x) V_R + \cosh(\gamma x) I_R$$

$$v = \frac{\omega}{\beta} \quad , \quad \lambda = \frac{v}{f}$$

Lossless line :

$$r=0 \quad , \quad g=0$$

$$Z = r + j\omega L \quad , \quad Y = g + j\omega C$$

$$\gamma = \alpha + j\beta \quad \text{with } r=0 \text{ and } g=0 \Rightarrow \gamma = j\beta$$

$$\gamma = \sqrt{ZY} = \sqrt{j\omega L + j\omega C} = j\omega \sqrt{LC}$$

$$\beta = \omega \sqrt{LC}$$

$$Z_c = \sqrt{\frac{Z}{Y}} = \sqrt{\frac{L}{C}}$$

→ in loss line  $\equiv$  pure resistance

$$v = \frac{\omega}{\beta} = \frac{\omega}{\omega \sqrt{LC}} = \frac{1}{\sqrt{LC}}$$



$$\lambda = \frac{v}{f} = \frac{1}{f\sqrt{LC}}$$

Neglecting Internal Flux :-

$$GMR_L = GMR_c$$

$$L = 2 \times 10^{-7} \ln \left( \frac{GMD}{GMR} \right)$$

$$C = \frac{2\pi\epsilon_0}{\ln \left( \frac{GMD}{GMR} \right)}$$

r  
r<sub>int</sub>  
Use GMD  
GMD<sub>int</sub>

$$v = \frac{1}{\sqrt{LC}} = \frac{1}{\sqrt{\mu_0\epsilon_0}} = 3 \times 10^8 \text{ m/s} \quad \text{speed of light}$$

$$\lambda = \frac{1}{f\sqrt{LC}} = \frac{1}{f\sqrt{\mu_0\epsilon_0}} = 5000 \text{ km}$$

60 Hz

$$Z_c = \sqrt{\frac{L}{C}} = \frac{1}{2\pi} \sqrt{\frac{\mu_0}{\epsilon_0}} \ln \left( \frac{GMD}{GMR_c} \right)$$

$$= 60 \ln \left( \frac{GMD}{GMR_c} \right)$$

$$\cosh(\gamma x) = \cosh(j\beta x) = \cos(\beta x)$$

$$\sinh(\gamma x) = \sinh(j\beta x) = j \sin(\beta x)$$



$Z_c \equiv \text{character impedance} \equiv \text{surge impedance}$

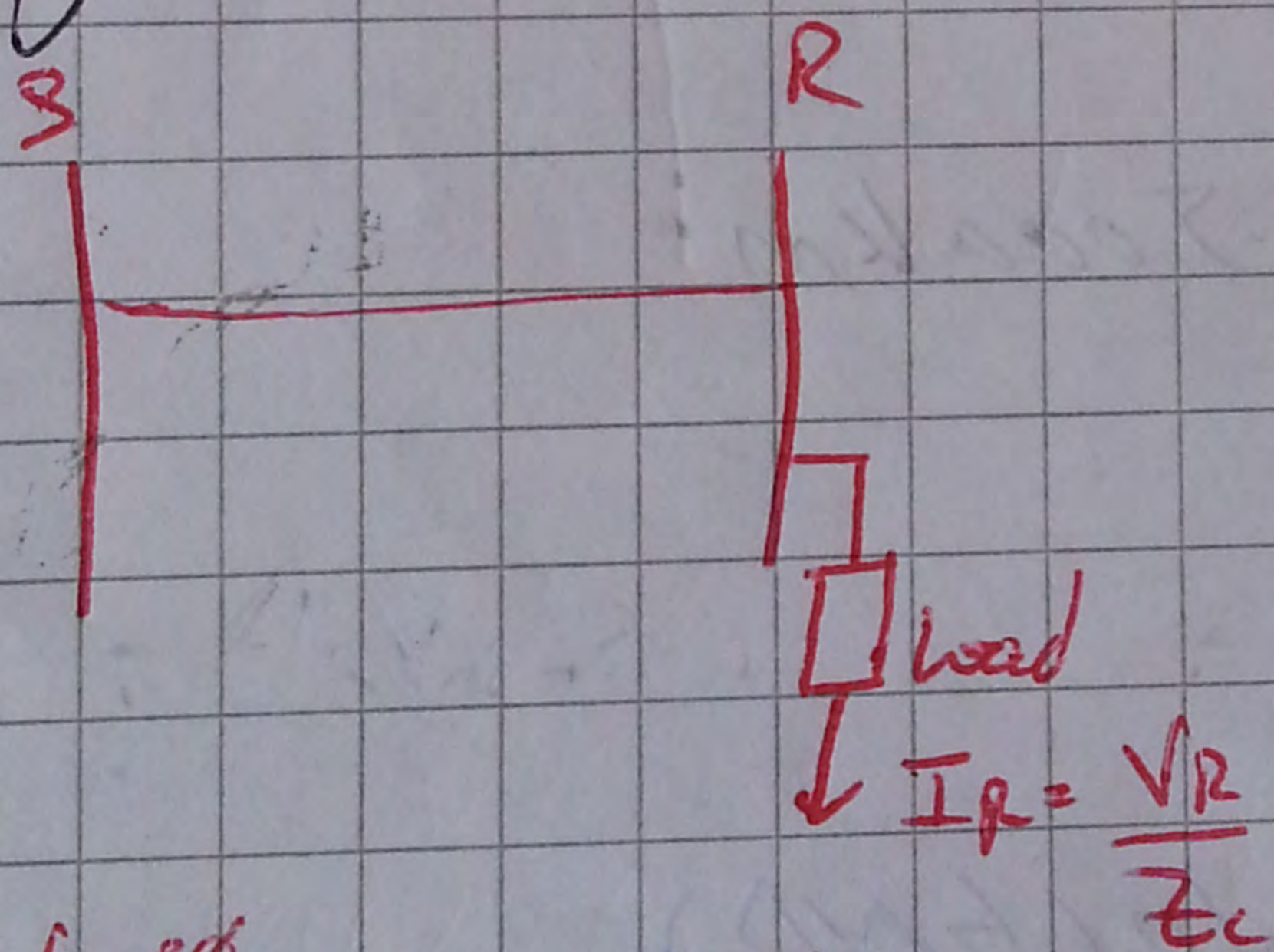
$$V(x) = \cos(\beta x) V_R + j Z_c \sin(\beta x) I_R$$

$$I(x) = j \frac{1}{Z_c} \sin(\beta x) V_R + \cos(\beta x) I_R$$

For typical T.L  $Z_c$  varies from 700  $\Omega$

for 69 kV — 250  $\Omega$  for double cat 765 kV

Surge Impedance Loading :



for 3 $\phi$   $\rightarrow$   $\text{ph-n}$

$$\begin{aligned} \text{SIL} &= 3 V_R I_R^* \\ &= \frac{3 V_R^2}{Z_c} \end{aligned}$$



$$SIL = 3 \left( \frac{V_{rL,L}}{\sqrt{3}} \right)^2 \frac{1}{Z_c} = \frac{V_{rL,L}^2}{Z_c} \text{ MW}$$

in The example of last lecture  
using lossless assumption

$$L = 230 \text{ mi}$$

$$z = 0.1603 + j0.8277$$

$$y = 5.105 \times 10^{-6} \text{ S/mi}$$

$$V_r = 124.13 \angle 0 \text{ kV}$$

$$I_r = 335.7 \angle 0 \text{ A}$$

$$z = jX_L \Rightarrow X_L = 0.8277 \Rightarrow L = \frac{0.8277}{2\pi f}$$

$$L = 2.1955 \text{ mH/mile}$$

$$\frac{1}{Z_c} = 5.105 \times 10^{-6} = \omega C \Rightarrow C = 1.35 \times 10^{-8} \text{ F/mile}$$

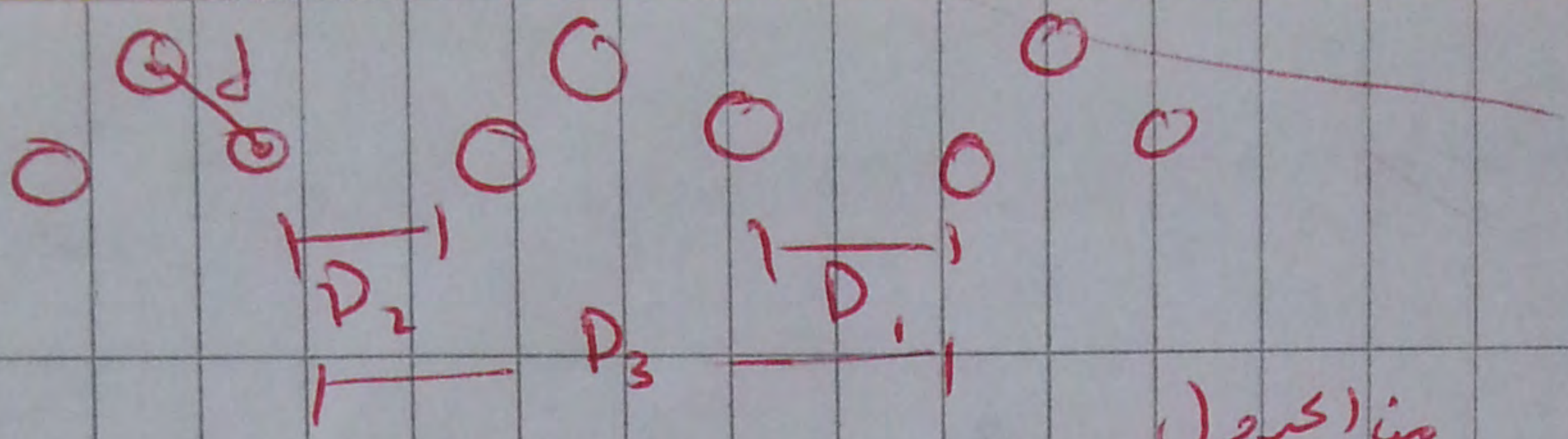
$$\alpha l = l \sqrt{Z_c} = l \sqrt{j\omega L} = j 2.03 \times 10^{-3}$$

$$\beta l = 2.03 \times 10^{-3} \text{ rad/mile} \times 230 = \beta l = 4.669 \times 10^{-4} \text{ rad/mile}$$

$$Z_c = \sqrt{\frac{L}{C}} = 403.27 \Omega$$

$$V(r) = 124.12563$$





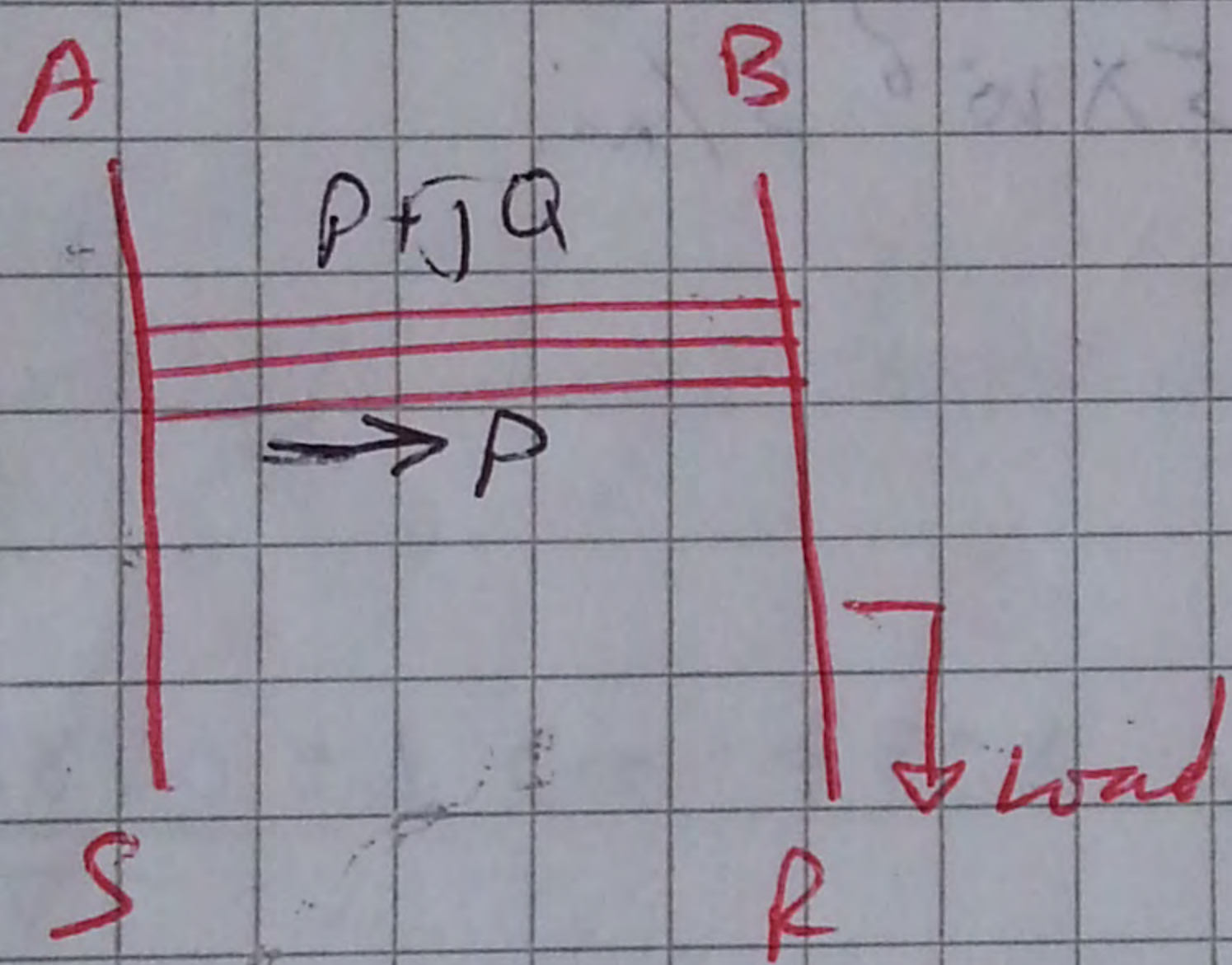
lecture 15

$$GMD = \sqrt[3]{D_1 D_2 D_3}$$

$$L_{MR} = \sqrt{GMR \times d^2}$$

$$L = 2 \times 10^{-7} \ln \left( \frac{GMD}{GMR} \right)$$

Complex power flow Through T.L :-



$$S = P + jQ$$

$$S = A \cos \theta$$

$$P = A \cos \theta$$

$$Q = A \sin \theta$$

(1)

$$V_s = A V_r + B I_r$$

$$A = |A| \angle \theta_A$$

$$B = |B| \angle \theta_B$$

$$V_r = |V_r| \angle 0^\circ$$

$$V_s = |V_s| \angle \delta$$

$$I_r = \frac{|V_s| \angle \delta - (|A| \angle \theta_A) (|V_r| \angle 0^\circ)}{|B| \angle \theta_B}$$



$$I_R = \frac{|V_s|}{|B|} \angle \delta - \theta_B - \frac{|A||V_R|}{|B|} \angle \theta_A - \theta_B$$

$$S_{R(3\phi)} = P_{R(3\phi)} + j Q_{R(3\phi)} = 3 V_{R,ph-n} I^*$$

$$S_{R(3\phi)} = \frac{3 |V_{R,ph-n}| |V_{s,ph-n}|}{|B|} \angle \theta_B - \delta - \frac{3 |V_{R,ph-n}| |A||V_R|}{|B|} \angle \theta_B - \theta_A$$

$$V_{ph-n} = \frac{V_L}{\sqrt{3}}$$

$$S_{R(3\phi)} = \frac{|V_{R(L-L)}| |V_{s(L-L)}|}{|B|} \angle \theta_B - \delta - \frac{|A||V_{R(L-L)}|^2}{|B|} \angle \theta_B - \theta_A$$

using (1)

$$P_{R(3\phi)} = \frac{|V_{R(L-L)}| |V_{s(L-L)}|}{|B|} \cos(\theta_B - \delta) - \frac{|A||V_{R(L-L)}|^2}{|B|} \cos(\theta_B - \theta_A)$$

$$Q_{R(3\phi)} = \frac{|V_{R(L-L)}| |V_{s(L-L)}|}{|B|} \sin(\theta_B - \delta) - \frac{|A||V_{R(L-L)}|^2}{|B|} \sin(\theta_B - \theta_A)$$



$$\begin{bmatrix} V_s \\ I_s \end{bmatrix} = \begin{bmatrix} A & B \\ C & D \end{bmatrix} \begin{bmatrix} V_R \\ I_R \end{bmatrix}$$

$$\begin{bmatrix} V_R \\ I_R \end{bmatrix} = \begin{bmatrix} D & -B \\ -C & A \end{bmatrix} \begin{bmatrix} V_s \\ I_s \end{bmatrix}$$

$$V_R = DV_s - BI_s$$

$$I_R = -CV_s + AI_s$$

$$[A=D]$$

$$V_R = DV_s - BI_s \Rightarrow I_s = \frac{AV_s - V_R}{B}$$

Lossless line

$$B = jZ_c \sin(\beta L)$$

$$A = \cos(\beta L)$$

Complex (B) is  $j\omega$   
only

$$\theta_B = 90^\circ - \omega$$

Real (A) is  
only

$$\theta_A = 0^\circ - \omega$$

$$\cos(\theta_B - \theta_A) = \cos(90) = 0$$

$$\cos(\theta_B - \delta) = \sin(\delta)$$



## power Transmission Capability :-

- 1) Thermal limit
- 2) Voltage limit
- 3) stability limit

$$S_{\text{Thermal}} = \text{Thermal loading limit} = 3 V_{\text{Rated}} I_{\text{Thermal}}$$

P.U = Actual power. unit  
Base

$$V_{R(p.u)} = \frac{V_R}{V_{\text{rated}}}$$

$$V_{S(p.u)} = \frac{V_S}{V_{\text{base}}}$$

$$R_{3\phi} = \left( \frac{|V_{R(p.u)}|}{|V_{\text{rated}}|} \right) \left( \frac{|V_{S(p.u)}|}{|V_{\text{rated}}|} \right) \left( \frac{V_{\text{rated}}^2 \sin \delta}{Z_c \sin(\beta L)} \right)$$

$$= |V_{R(p.u)}| * |V_{S(p.u)}| * SIL \quad \#$$

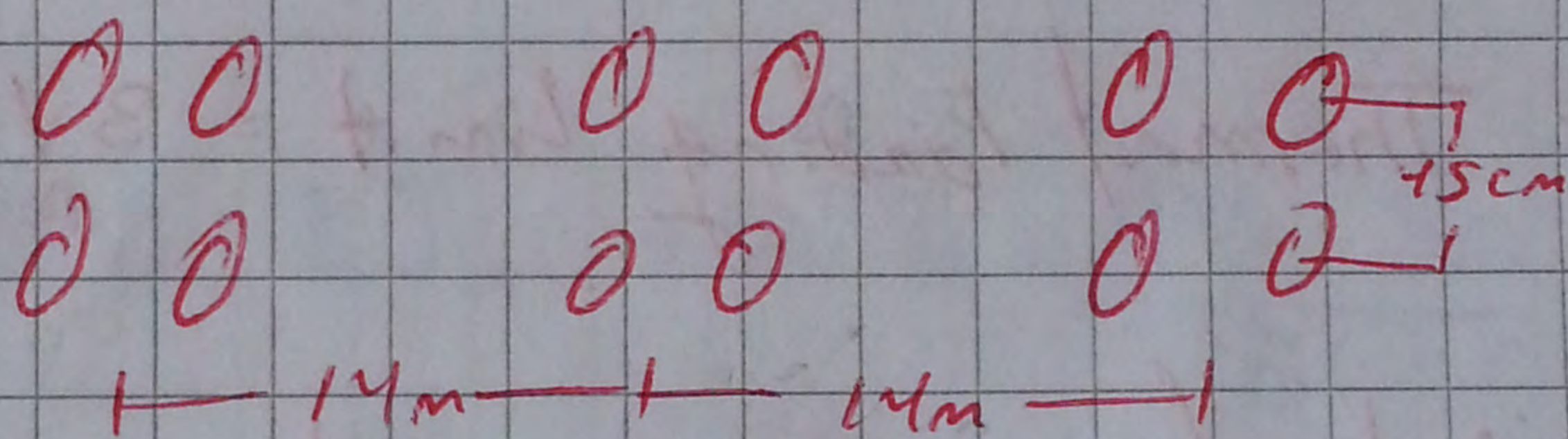
$$P_{3\phi} = \frac{|V_S|_{p.u} * |V_R|_{p.u} * SIL \sin \delta}{\sin \left( \frac{2\pi f}{\lambda} \right)}$$



lecture  
(16)

Ex (prob. 5.8 Snodgrass)

3 $\phi$ , 765 kV, 60 Hz transposed line 4 ACSR  
1,413,000 cmil, 45/7 RoboLink Cond per phase  
spacing (14m) diameter cond (3.625 cm) and



GMR = 1.439 cm (400 km) long (lossless line)

a)

$$Z_c = \sqrt{\frac{L}{C}}$$

$$GMD = \sqrt[3]{(14)(14)(28)} = 17.63 \text{ m}$$

$$GMR = 1.09 \sqrt[4]{45^3 \times 1.439} = 0.2075 \text{ m}$$

$$L = 0.2 \ln \left( \frac{GMD}{GMR} \right) = 0.2 \ln \left( \frac{17.63}{0.2075} \right) = 0.8885 \text{ mH/km}$$



ecture  
(16)

$$GMR_c = 1.09 \sqrt{\frac{45^3 \times 3.625}{2}} = 0.2198 \text{ m}$$

$$C = \frac{0.0556}{\ln\left(\frac{6.714}{GMR_c}\right)} = 0.01268 \mu\text{f/km}$$

ACSR

Phase

$$Z_c = \sqrt{\frac{0.8885 \times 10^{-3}}{0.01268 \times 10^{-6}}} = 264.7 \Omega$$

$$\beta = \omega \sqrt{LC} = 2\pi \times 60 \sqrt{0.8885 \times 10^{-3} \times 0.01268 \times 10^{-6}} \\ = 0.001265 \text{ rad/km}$$

$$\beta l = \frac{0.001265 \times 180}{\pi} \times 100 \\ = 29^\circ$$

$$\lambda = \frac{2\pi}{\beta} = \frac{2\pi}{0.001265} = 4967 \text{ km}$$

$$SIL = \frac{765^2}{Z_c} = \frac{V_L^2}{Z_c} = 2210.89 \text{ MW}$$

$$A = \cos(\beta l) = \cos(29^\circ) = 0.8746$$

$$B = j Z_c \sin(\beta l) = j (264.7) \sin(29^\circ) = j 128.33 \Omega$$

$$C = j \frac{1}{Z_c} \sin(\beta l) = j 0.00183 \text{ S}$$

85 mH/km



$$D = A = 0.8746$$

→ This equation in ph-n  
form only

$$5) V_s = A V_R + B I_R$$

$$V_R = \frac{735}{\sqrt{3}} = 424.35 \angle 0^\circ \text{ kV}$$

$$I_R = \frac{2000 \times 10^6}{\sqrt{3} \times 735 \times 10^3} = 1.571 \text{ kA} \angle -36.87^\circ$$

$$F_p = 0.8 \text{ lagging} \\ \cos^{-1}(0.8) = 36.87^\circ$$

$$|V_{s(L.L)}| = \sqrt{3} (518.86) = 896.96 \text{ kV}$$

$$V_s = (0.8746) 424.35 + j 128.33 \times 1.571 \angle -36.87^\circ \\ = 518.86 \angle 18.15^\circ \text{ kV}$$

$$I_s = C V_R + D I_R$$

$$= j 0.00183 \times 424.35 \angle 0^\circ + 0.8746 \times 1.57 \angle -36.87^\circ$$

$$= 1.1 \angle -2.46^\circ$$

$$18.15 - (-2.46) = 20.6^\circ$$

$$1/P_s = \cos(20.6) =$$

$$S_{3\phi \text{ sending}} = \sqrt{3} \times 896.96 \angle 18.15^\circ \times 1.1 \angle 2.46^\circ$$



any value of voltage given is Line to Line

$$S_{3\phi} = 3 V_s I_s^*$$

$$= 3 \times 518.86 \angle 18.15^\circ \times 1.1 \angle 2.46^\circ$$

$$= 1709.3 \angle 20.6^\circ \text{ MVA}$$

$$= 1600 \text{ MW} + j 601.59 \text{ MVAR}$$

$$V_R = \frac{V_{R(LN)} - V_{R(FL)}}{V_{R(F.L.)}}$$

$$= \frac{\frac{896.96}{0.8746} - 735}{735} = 39.53\%$$

$$c) \begin{pmatrix} V_s \\ I_s \end{pmatrix} = \begin{pmatrix} A & B \\ C & D \end{pmatrix} \begin{pmatrix} V_R \\ I_R \end{pmatrix}$$

$$AD - BC = 1$$

$$\begin{pmatrix} V_R \\ I_R \end{pmatrix} = \begin{bmatrix} D & -B \\ -C & A \end{bmatrix} \begin{pmatrix} V_s \\ I_s \end{pmatrix}$$

$$V_R = DV_s - BI_s$$

$$V_s = \frac{465}{\sqrt{3}} = 441.67 \text{ kV} \angle 0^\circ$$



$$S_s = \sqrt{1920^2 + 1600^2} = 2011.57 \text{ MVA } \angle 17.35^\circ$$

$$S_{1\phi} = V \cdot I^*$$

$$= \frac{S^*}{\sqrt{3}} = \frac{(2011.57/3) \times 10^6 \angle -17.35^\circ}{441.67 \angle 0^\circ}$$

$$1.518 \text{ kA } \angle -17.35^\circ$$

$$V_R = DV_s - BI_s = 377.2 \angle -29.5^\circ \text{ kV}$$

$$|V_{R_{LL}}| = \sqrt{3} (377.2) = 653.329 \text{ kV}$$

$$I_R = -CV_s + AI_s = 1.749 \text{ kA } \angle -43.55^\circ$$

$$S_{R(3\phi)} = 3 V_R I_R^* = 1978.86 \angle 14^\circ \text{ MVA}$$

$$= 1920 \text{ MW} + j 479.2 \text{ MVAR}$$



# Solution of last example (cont)

lecture  
(17)

d)  $V_s, I_s, P_s, S$  with  $R_L = 264.5 \Omega$  and  $V_R = 735 \text{ mV}$

$$V_s = A V_R + B I_R$$

$$\frac{V_R}{\sqrt{3}} = \frac{735}{\sqrt{3}} = 424.35 \angle 0^\circ \text{ mV (ph-n)}$$

$$I_R = \frac{V_R}{R} = \frac{424.35 \times 10^{-3}}{264.5} = 1604.3478 \angle 0^\circ$$

$$V_s = A V_R + B I_R = 424.42 \angle 29.02^\circ \text{ mV}$$

$$I_s = C V_R + D I_R = 1604.04 \angle 28.98^\circ \text{ A}$$

$$P_{12} = \cos(29.02 - 28.98) = 0.999 \approx \pm 1 \text{ unity power factor}$$

$$S_{3\phi} = 3 V_s I_s^*$$

$$= 3 (424.42 \angle 29.02^\circ) (1604.04 \angle -28.98^\circ)$$

$$= 2042.4 \angle 0.04^\circ \text{ MVA}$$

$$= 2042.4 \text{ MW} + j 1.4 \text{ MVAR}$$



$$V.R = \frac{\frac{735.12}{0.8748} - 735}{735} \times 100 = 14.36\%$$

A ←

prob 5-18

power system studies on an existing system have indicated that 2400 MW are to be transmitted for distance of 400 km, the voltage level being considered include 345 kV, 500 kV and 765 kV for a preliminary design based on the practical line, loadability you may assume the following surge impedance

|        |                    |        |                    |
|--------|--------------------|--------|--------------------|
| 345 kV | $Z_c = 320 \Omega$ | 765 kV | $Z_c = 265 \Omega$ |
| 500 kV | $Z_c = 290 \Omega$ |        |                    |



$$V.R = \frac{735.12}{0.8746} - 735 \times 100 = 14.36\%$$

A ←

prob 5-18

power system studies on an existing system have indicated that 2400 MW are to be transmitted for distance of 400 km, the voltage level being considered include 345 kV, 500 kV and 765 kV for a preliminary design based on the practical line, loadability you may assume the following surge impedance

|        |                    |        |                    |
|--------|--------------------|--------|--------------------|
| 345 kV | $Z_c = 320 \Omega$ | 765 kV | $Z_c = 265 \Omega$ |
| 500 kV | $Z_c = 290 \Omega$ |        |                    |



The line wave length may be assumed to be 5000 km, the practical line loadability may be based on a load angle of  $(35^\circ)$  assume

$|V_s| = 1.0 \text{ p.u.}$  and  $|V_r| = 0.9 \text{ p.u.}$ . Determine

the number of 3-phase transmission circuits required for each voltage level, each P. transmission tower may have up to 2 cct's

To limit the corona loss, all 500 kV line must have at least 2 conductors/phase

and all 765 kV lines must have at least

4 conductors/phase, The bundle spacing is 45 cm, the cord size should be such

that the line would be capable of carrying current corresponding to at least 5000 MVA



چهار کای = دو قطر اقل

ال power ال  
ثقله نقلها ال  
ال power ال

ال power ال  
SIL

$$P_{3\phi} = \frac{|V_s|_{pu} + |V_2|_{pu} + SIL}{\sin\left(\frac{2\pi}{3}\right)}$$

375 MW

$$SIL = \frac{K \sqrt{L_{12}}^2}{Z_c}$$

$$= \frac{345^2}{320} = 371.95 \text{ MVA}$$

$$P_{3\phi} = \frac{1 + 0.9 + 371.95}{\sin\left(\frac{2\pi \cdot 400}{5000} \times \frac{180}{\pi}\right)} \sin(135^\circ)$$

28.8°

$$\approx 400 \text{ MW}$$

$$\# \text{ of cct's} = \frac{2400}{4} = 6 \text{ circuits}$$

$$\# \text{ of towers} = \frac{6}{2} = 3 \text{ towers}$$



$$V_1 = +3\% = 1.03 \text{ pu}$$

$$V_2 = -4\% = 0.96 \text{ pu}$$

500 kV

$$S_{TL} = \frac{500^2}{290} = 862.07 \text{ MVA}$$

$$P_{sp} = \frac{1 + 0.9 + 862.07 \sin(35)}{\sin(28.8)} = 923.3 \text{ MW}$$

$$\# \text{ of circuits} = \frac{2400}{923.3} = 2.6 \Rightarrow 3 \text{ circuits}$$

$$\# \text{ of towers} = \frac{3}{2} = 1.5 \Rightarrow 2 \text{ towers}$$

765 kV

$$S_{TL} = \frac{765^2}{265} = 2208.4 \text{ MVA}$$

$$P_{sp} = \frac{1 + 0.9 + 2208.4 \sin(35)}{\sin(28.8)} = 2365.2 \text{ MW}$$

$$\# \text{ of circuits} = 1 \text{ circuit}$$

$$\# \text{ of towers} = 1 \text{ tower}$$

So 765 is the best one

$$I = \frac{5000}{\sqrt{3} \times 765} = 3773.5 \text{ A / phase}$$

$$I = \frac{3773.5}{4} = 943.38 \text{ A / conductor}$$

From table see which and here this value



شانت كابتيسر  
Shunt Capacitor  
نظير T.L (مكافئ) يلا ينقسم

كيف نظير  $X_L$  او  $X_C$  نظير

Lecture  
(18)

# Line Compensation

Shunt reactor

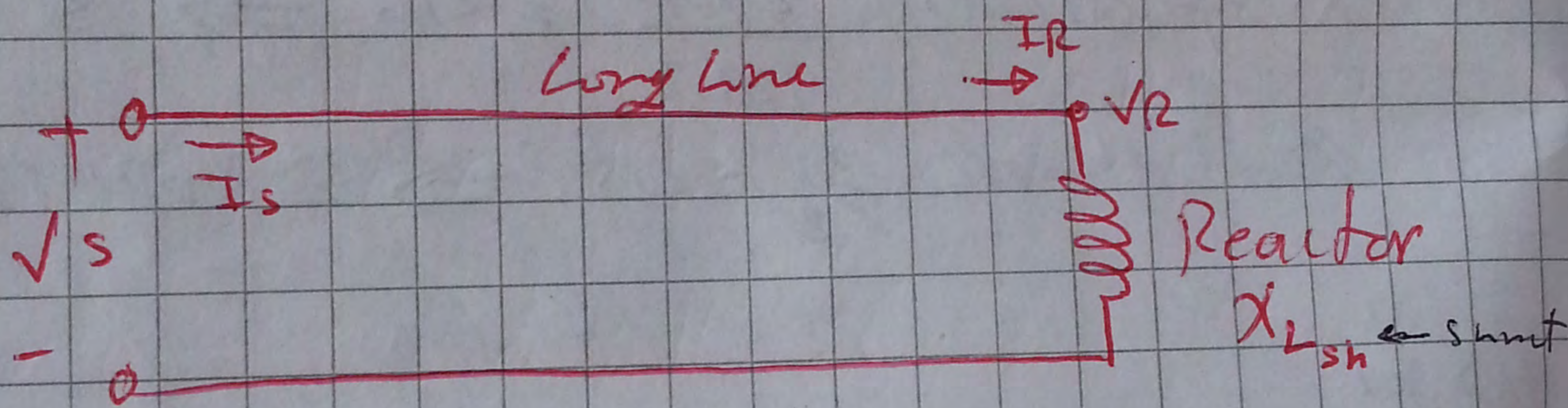
↓ V

Light Load (no load) so  
voltage increase

Shunt capacitor

↑ V

(Loaded line)  
Low voltage so  
add capacitor



$$I_R = \frac{V_R}{jX_{L_{sh}}} \quad (1)$$

$$V_s = A V_R + B I_R$$

$$= \cos(\beta l) V_R + j Z_c \sin(\beta l) I_R \quad (2)$$

lossless

sub (1) in (2)

$$V_s = \left[ \cos(\beta l) + \frac{Z_c \sin(\beta l)}{X_{L_{sh}}} \right] V_R \quad (3)$$



Assume  $V_R$  and  $V_S$  are in phase

So the power through T.L is zero

From (3)

$$X_{L_{sh}} = \frac{\sin(\beta l)}{\frac{V_S}{V_R} - \cos(\beta l)} Z_c \quad \text{--- (6)}$$

For  $V_S = V_R$

$$X_{L_{sh}} = \frac{\sin(\beta l)}{1 - \cos(\beta l)} Z_c$$

To find the relation between  $I_S$  and  $I_R$

$$I_S = C V_R + D I_R$$

$$= j \frac{1}{Z_c} \sin(\beta l) V_R + \cos(\beta l) I_R \quad \text{--- (4)}$$

Sub (1) in (4)

$$V_S = \left[ -\frac{1}{Z_c} \sin(\beta l) X_{L_{sh}} + \cos(\beta l) \right] I_R \quad \text{--- (5)}$$



sub (6) in (5)

$$I_s = -I_R$$

at mid span  
(T.L.  $\rightarrow$  (open))  
 $I=0$

$$V_m = \frac{V_R}{\cos(\beta \frac{L}{2})}$$

mid point

Example 8 For T.L of EXL) calculate <sup>in lecture 13</sup>

- a) the receiving end voltage when line is terminated in an open circuit and is energized with 500 kV at the sending end
- b) Determine the reactance and MVAR of 3 $\phi$  shunt reactor to be installed at the receiving end to keep the no load receiving end voltage at the rated value



$$Z_L = 290.43 \Omega$$

$$\beta L = 21.64$$

$$V_s = 500 \text{ kV}$$

$$\text{open ct} \Rightarrow I_R = 0 \text{ (no load)}$$

the receiving end voltage

$$V_{R(NL)} = \frac{V_s}{A} = \frac{288.675 \times 10^3}{0.9295} = 310.57 \text{ kV (ph-n)}$$

$$V_s = \frac{500}{\sqrt{3}} = 288.675 \text{ kV}$$

$$A = \cos(\beta L) = 0.9295$$

$$|V_{R(NL)}|_{L-L} = \sqrt{3} (310.57) = 537.9 \text{ kV}$$

$$X_{L_{sh}} = \frac{\sin(21.64)}{1 - \cos(21.64)} \times 290.43$$

$$= 1519.5 \Omega$$

$$Q = \frac{V_{LL}^2}{X} = \frac{500^2}{1519.5} = 164.53 \text{ MVAR}$$

For 3φ



no load, in series with reactor (series s.w.)  
 capacitor

lecture  
(19)

## shunt capacitor compensation

$$P_{R(3\phi)} = \frac{|V_{S(L,L)}| |V_{R(L,L)}| \cos(\theta_B - \delta)}{|B|} - \frac{|A| |V_{R(L,L)}|^2 \cos(\theta_B - \theta_A)}{|B|}$$

$$P_{R(3\phi)} = \frac{|V_{S(L,L)}| |V_{R(L,L)}| \sin \delta}{X} \quad \text{Lossless Line}$$

$$Q_{R(3\phi)} = \frac{|V_{S(L,L)}| |V_{R(L,L)}| \sin(\theta_B - \delta)}{|B|} - \frac{|A| |V_{R(L,L)}|^2 \sin(\theta_B - \theta_A)}{|B|}$$

$$Q_{R(3\phi)} = \frac{|V_{S(L,L)}| |V_{R(L,L)}| \cos \delta}{|B|} - \frac{|V_{R(L,L)}|^2 \cos(\beta_1)}{X} \quad \downarrow \text{Lossless Line}$$

(X' = B)

## Series capacitor compensation :-

- 1) Are connected in series with the line
- 2) Are located at the mid point of the line  
used for :-
- 1) are used to reduce the series reactance



lecture  
(19)

$$\text{Percentage Compensation} = \frac{X_{c_{ser}}}{X}$$

between the load and supply point

- 2) Improve steady state and transient stability
- 3) More economical loading
- 4) Minimum voltage dip on load buses

**Example 8** A transmission line in Excs. 5 lecture (13)

supplies a load of 1000 MVA, 0.8 p.f lagging at 500 kV, a) Determine the MVAR and the capacitance of the shunt capacitor to be installed at the receiving end voltage at 500 kV when the line is energized with 500 kV at the sending end

b) only series capacitor are installed at the mid point of the line providing 40% compensation, find the sending end voltage and V.R



Lagging = inductive load  
leading = capacitive load

$$Z_c = 290.43 \Omega, \beta_1 = 21.64^\circ$$

$$\cos^{-1}(0.8) = 36.87^\circ$$

$$S = 1000 \angle 36.87^\circ = 800 \text{ MW} + j 600 \text{ MVAR}$$

$$\begin{aligned} a) \quad B = X &= Z_c \sin(\beta_1) = 290.43 * \sin(21.64) \\ &= 107.11 \Omega \end{aligned}$$

$$P_{(3\phi)} = \frac{|V_{S(L-L)}| |V_{R(L-L)}|}{X} \sin \delta$$

$$800 \text{ MW} = \frac{(500 \text{ kV})(500 \text{ kV})}{107.11} \sin \delta$$

$$\delta = 20.04^\circ$$

$$Q_{(3\phi)} = \frac{|V_{S(L-L)}| |V_{R(L-L)}|}{|B|} \cos(\delta) - \frac{|V_{R(L-L)}|^2}{X} \cos(\beta_1)$$

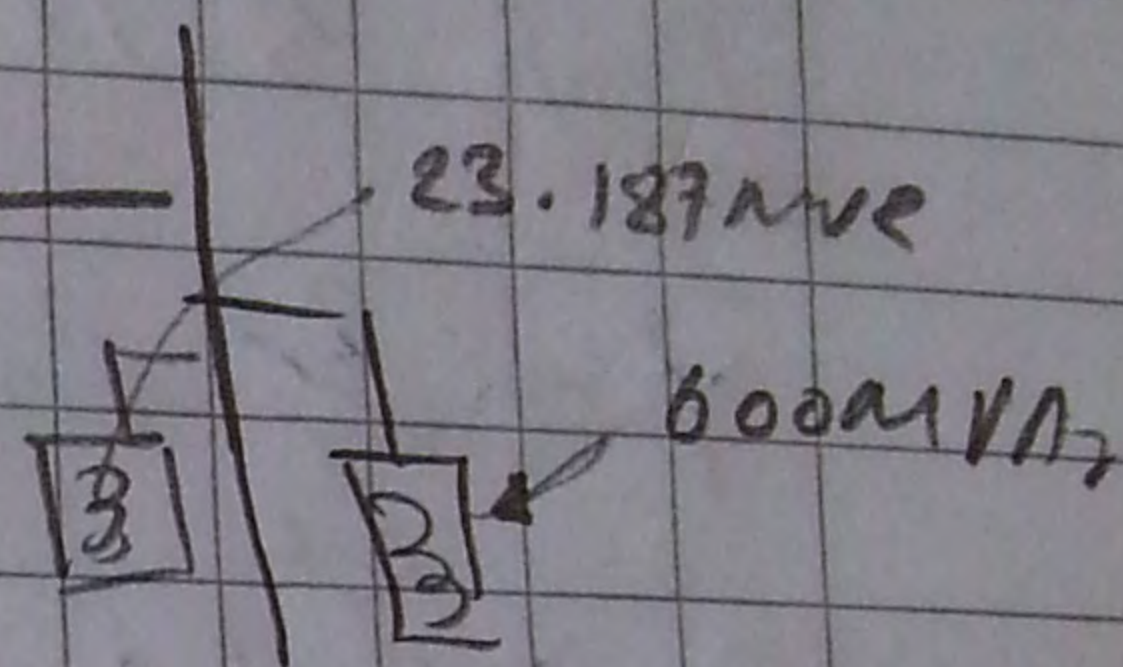
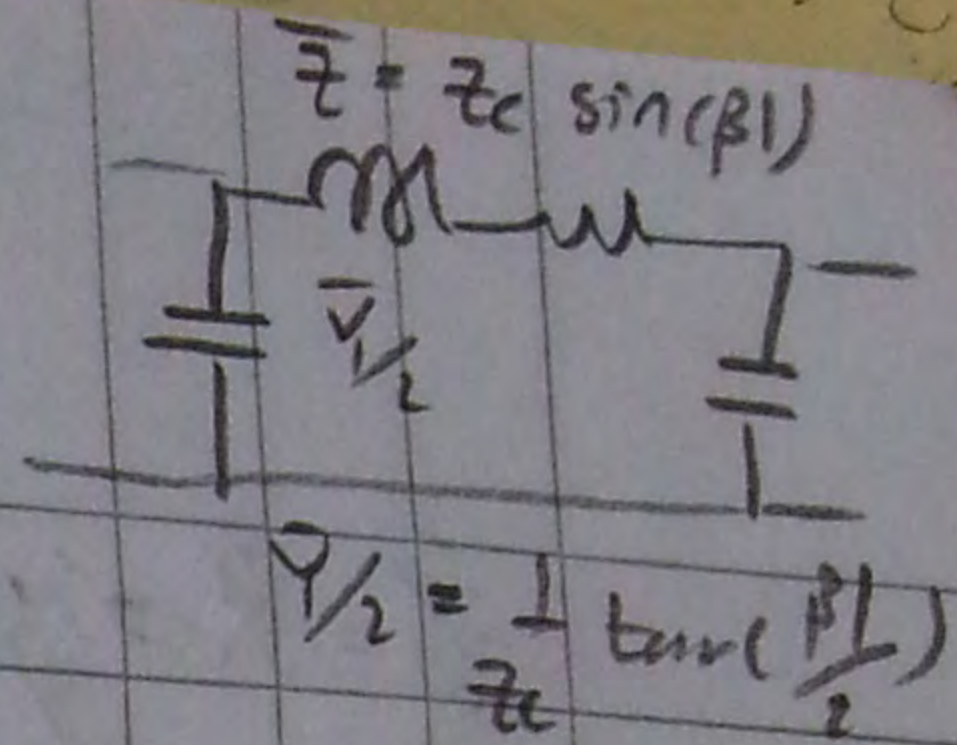
$$= \frac{(500 \text{ kV})(500 \text{ kV})}{107.11} \cos(20.04) - \frac{500^2}{107.11} \cos(21.64)$$

$$= 23.187 \text{ MVAR}$$



+ve - cosine (leading)  $P_f$   $Q_f$

at the receiving end



The required capacitor MVAR

$$P_f \text{ (lagging)} = j23.187 \times 600 = -j576.85 \text{ MVAR}$$

$$X_c = \frac{V_R^2}{Q} = \frac{500^2}{576.85} = 433.38 \Omega$$

$$C = \frac{1}{\omega X_c} = \frac{1}{2\pi \times 60 \times 433.38} = 6.1 \mu\text{f}$$

b)

$$40\% = \frac{X_{c \text{ ser}}}{X} = \frac{X_{c \text{ ser}}}{107.11} \Rightarrow X_{c \text{ ser}} = 42.84 \Omega$$

سلسلة (B), (A) في compensation, 1, 2, 3 (أدلة  
أو

$$V_s = AV_R + BIR$$

$$A = 1 + \frac{\bar{Z}\bar{Y}}{2}, \quad B = \bar{Z}, \quad C = \bar{Y}(1 + \frac{\bar{Z}\bar{Y}}{2})$$

$$D = A$$



$$S = 3 V_R I^*$$

$$\bar{Z} = \bar{Z} = j107.11 - j42.84 = j64.27 \Omega$$

$$\bar{Y} = \frac{2}{Z_c} \tan\left(\frac{\beta l}{2}\right) = \frac{2}{290.43} \tan\left(\frac{21.04^\circ}{2}\right)$$

$$\bar{Y} = 0.001316 \text{ S}$$

$$A = 1 + \frac{\bar{Z}\bar{Y}}{2} = 0.9577$$

$$B = \bar{Z} = j64.27 \Omega$$

$$V_R = \frac{500 \text{ W}}{\sqrt{3}} = 288.675 \text{ W} \angle 0^\circ$$

$$I_R = \frac{1000 \angle -36.87^\circ}{3 \times 288.675 \angle 0^\circ} = 1.155 \angle -36.87^\circ \text{ A}$$

$$V_S = 326.4 \angle 10.47^\circ \text{ W}$$

$$|V_{S(UL)}| = \sqrt{3} (326.4) = 565.4 \text{ W}$$

$$\%VR = \frac{V_R(NL) - V_R(FL)}{V_R(FL)} \times 100$$

$$V_R(NL) = \frac{V_S}{A} = \frac{565.4}{0.9577} = 590.37 \text{ W}$$

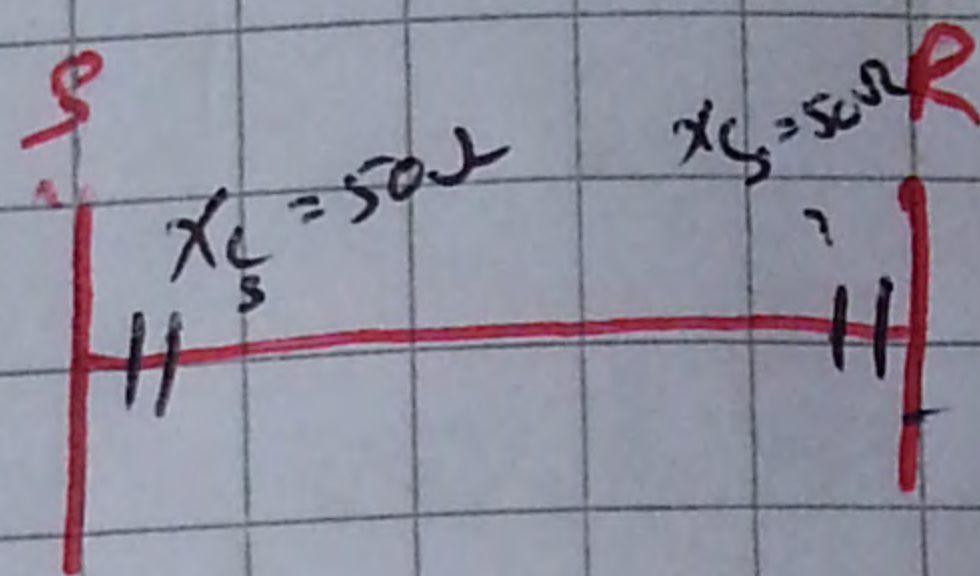


$$\%VR = \frac{590.37 - 500}{500} \times 100 = 18\%$$



Prob 5-15 Saadat

Lecture (20)



1000 MVA  
 $P_f = 0.8$  lagging  
 500 W

$$A = D = 0.86 + j0.0$$

$$B = 0 + j130.2 \Omega$$

$$C = j0.002 \text{ S}$$

a)  $V_s, I_s, P_s, S_s$  and  $V_R$

b) by adding series capacitor at the two ends

Find  $A'B'C'D$  constant

$$\begin{bmatrix} A' & B' \\ C' & D' \end{bmatrix} = \begin{bmatrix} 1 & -j50 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 0.86 & j130.2 \\ j0.002 & 0.86 \end{bmatrix} \begin{bmatrix} 1 & -j50 \\ 0 & 1 \end{bmatrix}$$

$$= \begin{bmatrix} 0.96 & j39.2 \\ j0.002 & 0.96 \end{bmatrix}$$

$$V_{s_{\text{new}}} = A'V_s + B'I_R$$

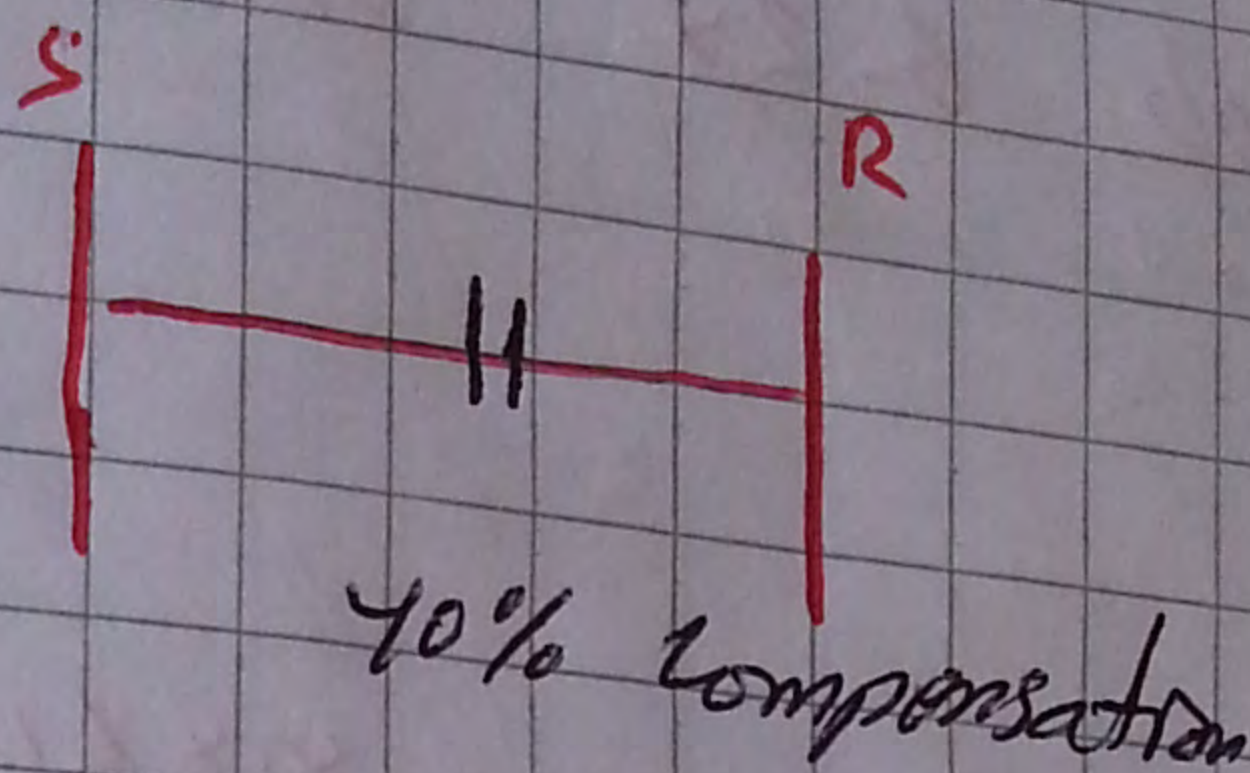


Prob 5-12 Saadat

$$B = X = 128.33 \Omega$$

$$\beta = 29$$

$$Z_c = 264.7 \Omega$$



$$40\% = \frac{X_{c \text{ series}}}{X}$$

$$X_{cs} = 0.4 \times 128.33 = 51.33 \Omega$$

$$C = \frac{1}{\omega X_c} = 51.67 \mu F$$

$$\bar{Z} = j(128.33 - 51.33) = j77 \Omega$$

$$\bar{Y} = \frac{2}{j/Z_c} \tan(\beta l / 2) = \frac{2}{j264.7} \tan(29/2) = j0.001954$$

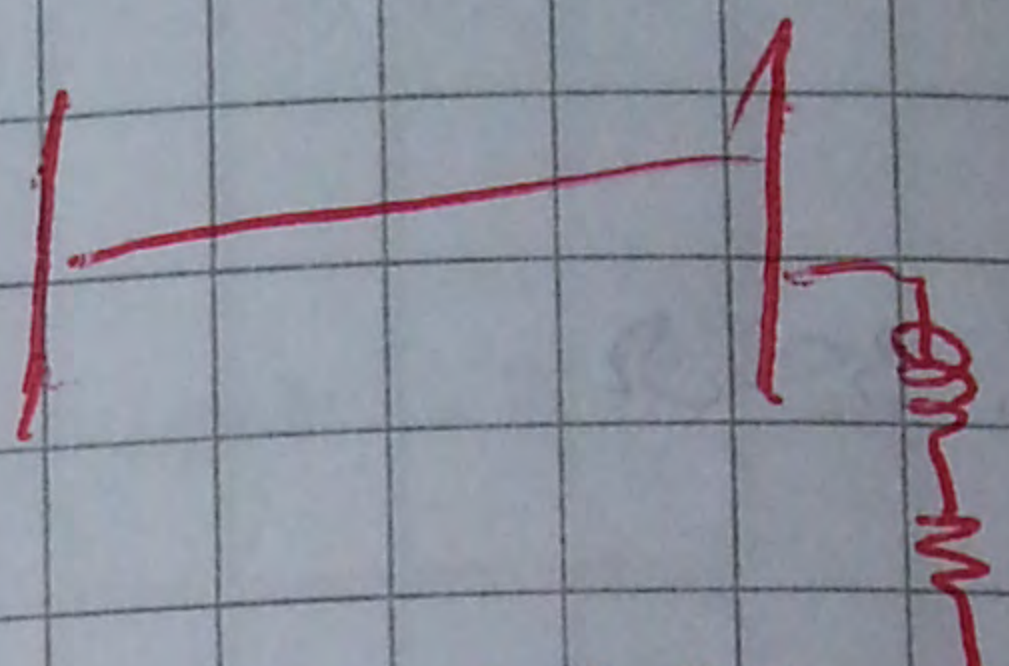
$$A = 1 + \frac{(j77)(j0.00195)}{2} = 0.92476$$

$$B = \bar{Z} = j77 \Omega$$

$$C = \bar{Y} (1 + \bar{Z} \bar{Y} / 4) = 0.00188$$



prob 6-25 Stev



250 MVA  
345 MVA

$$\begin{bmatrix} A & B \\ C & D \end{bmatrix} = \begin{bmatrix} 0.818 \angle 1.3 & 172.2 \angle 84.2 \\ 0.001933 \angle 90.4 & 0.818 \angle 1.3 \end{bmatrix}$$

$$X_L = \frac{345}{250} = 476.1 \angle 90$$

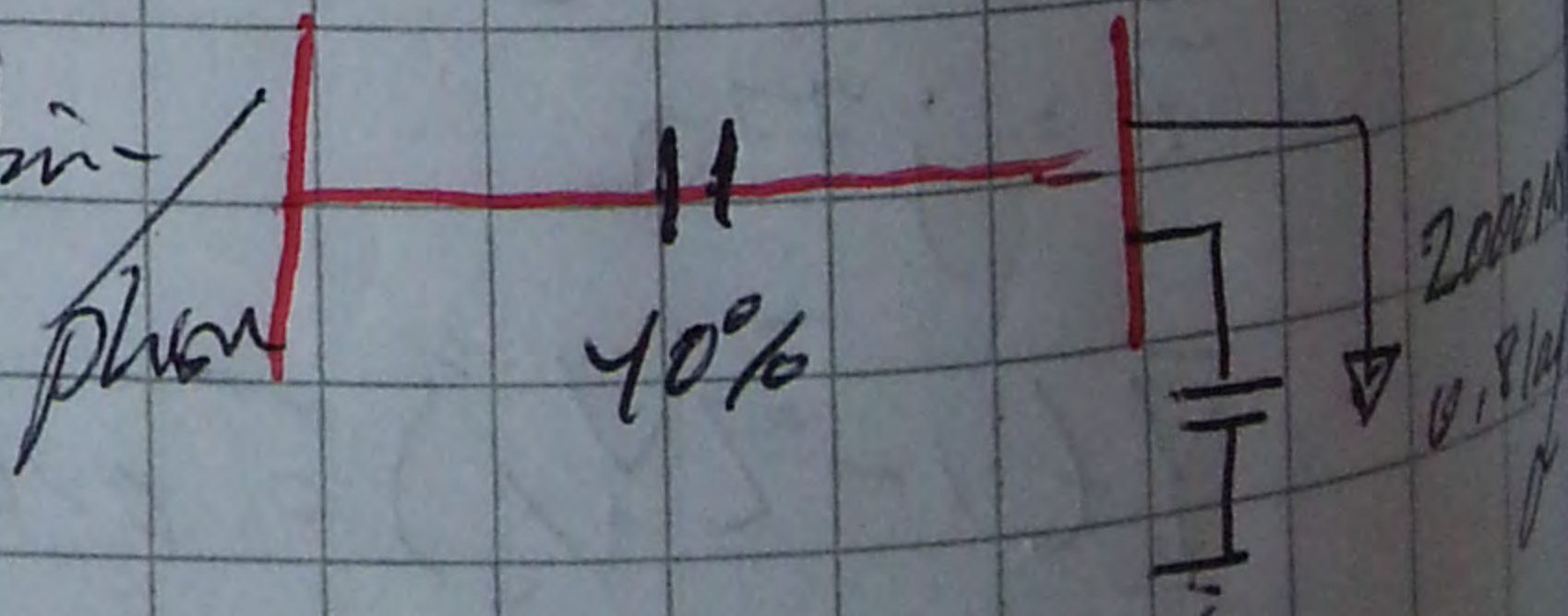
$$B_L = \frac{1}{X_L} = \frac{1}{476.1 \angle 90} = 0.0021 \angle -90 = -j0.0021$$

$$\begin{bmatrix} \hat{A} & \hat{B} \\ \hat{C} & \hat{D} \end{bmatrix} = \begin{bmatrix} A & B \\ C & D \end{bmatrix} \begin{bmatrix} 1 & 0 \\ -j0.0021 & 1 \end{bmatrix}$$

$$= \begin{bmatrix} 1.178 \angle -0.88 & 172.2 \angle 84.2 \\ 0.000217 \angle 83.25 & 1.178 \angle -0.88 \end{bmatrix}$$

prob

Find total MVA and capacitor  
of series and shunt capacitor  
to keep  $V_R = 735$  kV where  
 $V_S = 785$  kV where  $X = 128.33 \Omega$



2000 MVA  
0.818 MVA



$$P_{\frac{P}{3\phi}} = \frac{|V_s| |V_R|}{X} \sin \delta$$

$$Q_{\frac{P}{3\phi}} = \frac{|V_s| |V_R|}{1.81} \cos \delta - \frac{|V_R|^2}{X} \cos(\beta_1)$$

Line-line

$$2000 \angle 36.86^\circ = 1600 + j1200$$

$$1600 = \frac{(765)(735)}{1.771} \sin \delta$$

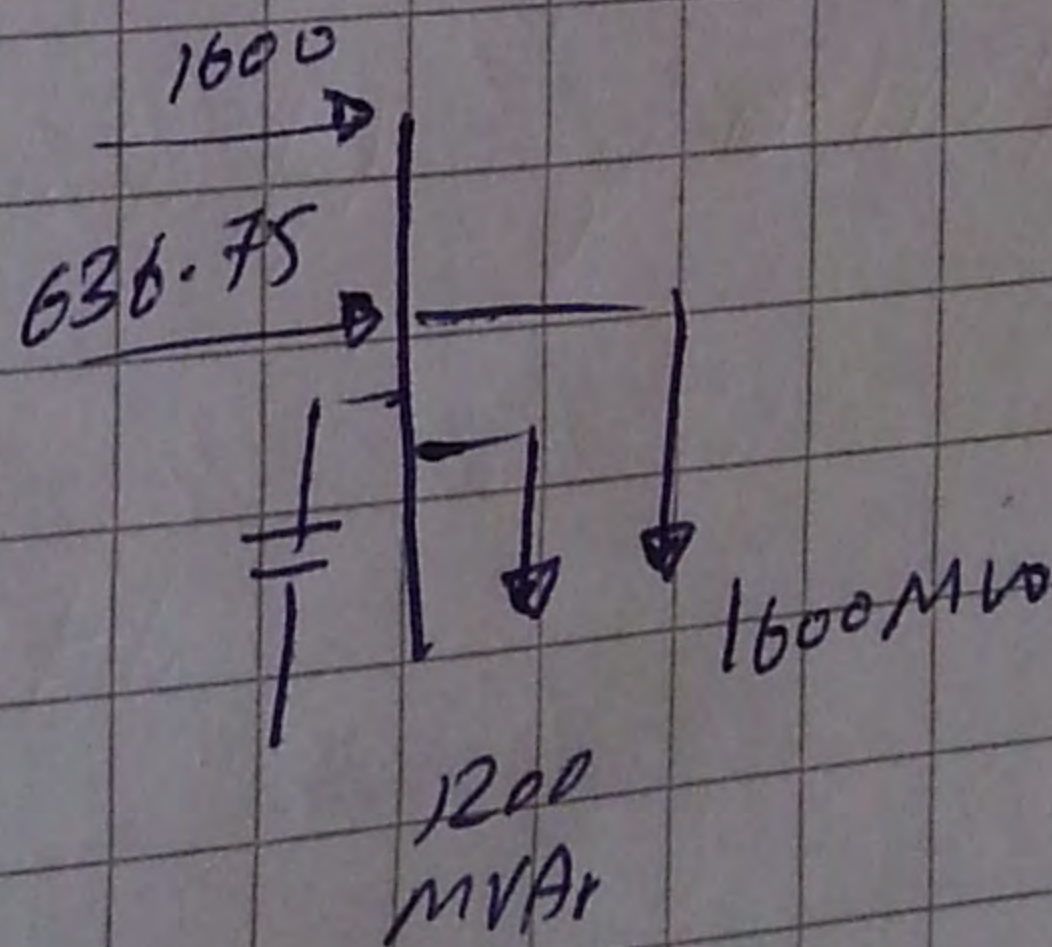
$$\delta = 12.856^\circ$$

$$\begin{aligned} X_{\text{new}} &= 128.33 \\ &- 0.1(128.33) \\ &= j77.2 \end{aligned}$$

$$Q_{\frac{P}{3\phi}} = \frac{(765)(735) \cos(21.856)}{1.77} - \frac{(735)^2}{77} \cos(29)$$

$$= 636.75 \text{ MVAR}$$

$$j636.75 - j1200 = -j563.25 \text{ MVAR}$$



$$X_c = \frac{735^2}{563.25} = -j959.12 \Omega$$

2000 MVA  
0.8 lag  
 $\alpha$



$$S_R = 1600 + j 636.75$$

$$I_{R_{new}} = \frac{S_R^*}{3 \sqrt{2}}$$

$$I_{R_{new}} \quad (A)$$

see problem 6.6 step (8)